

# Spatial Data

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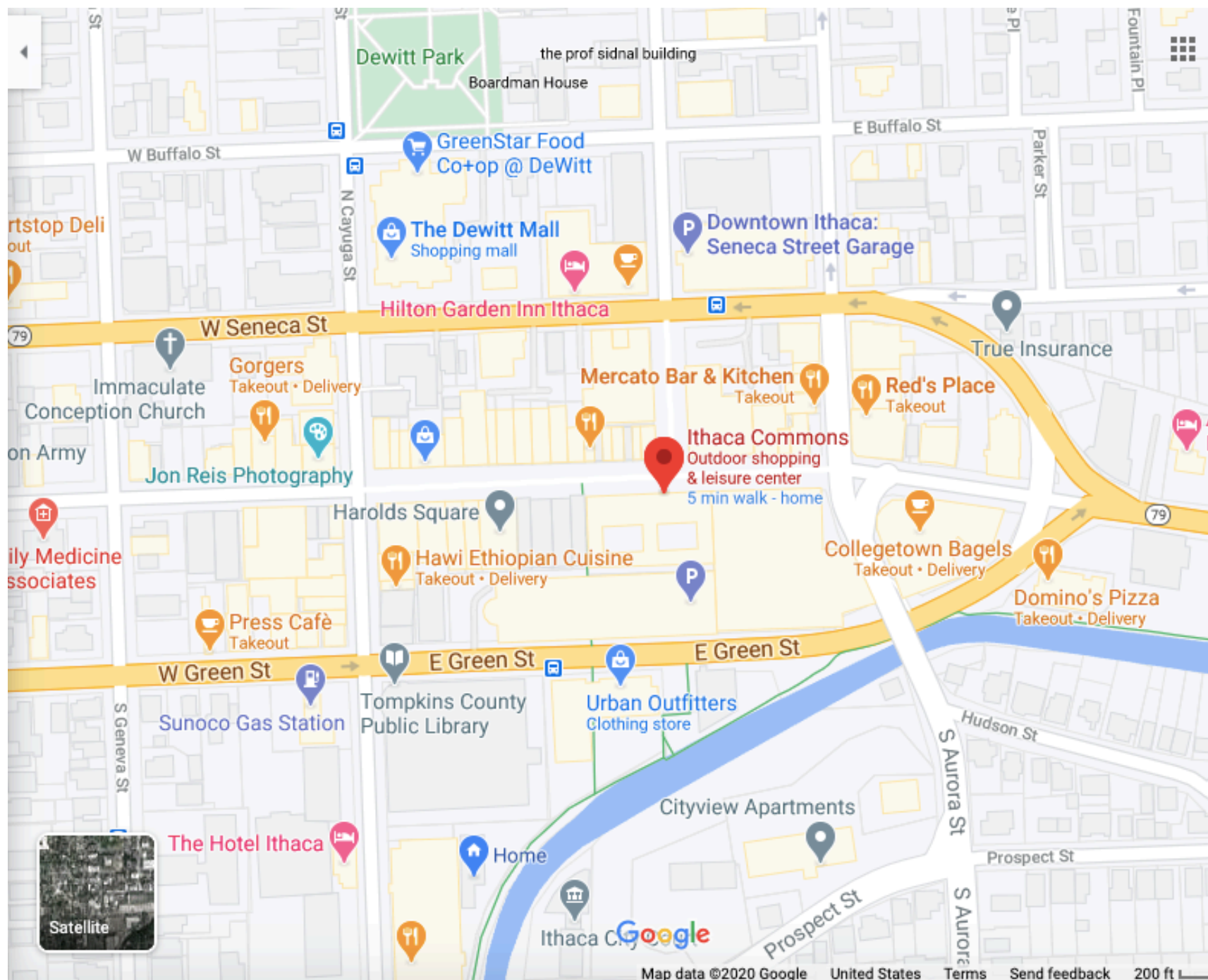
**[RG, Sec. 28]**

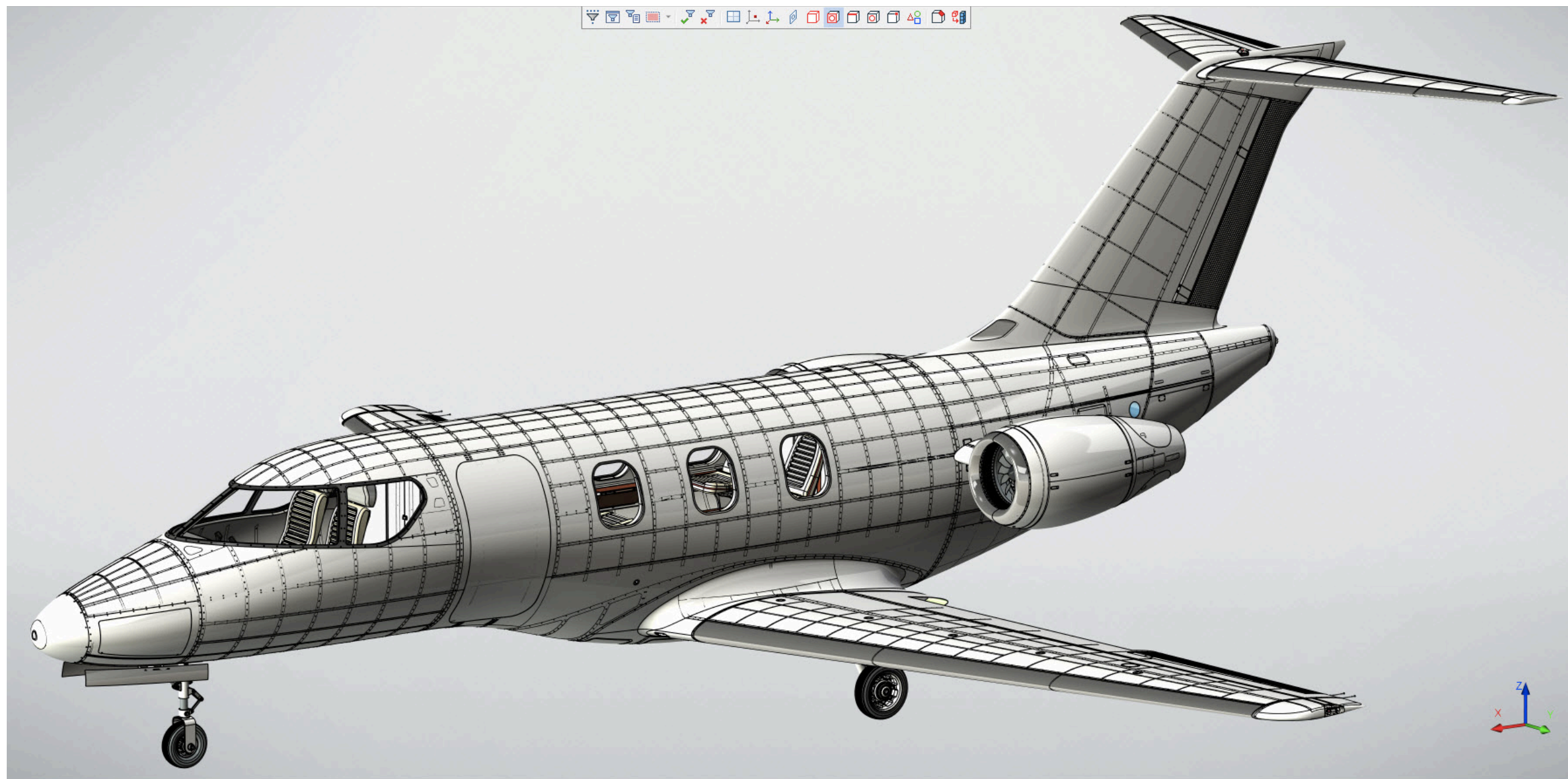
# Outlook: Beyond Relational Data

- Graph data
- Data streams
- Spatial data

# Outlook: Beyond Relational Data

- Graph data
- Data streams
- **Spatial data**





*Source: Wikipedia*

# Types of Spatial Data

- **Point** data
  - Characterized completely by the location
- **Region** data
  - Defined by a boundary (e.g., line or surface)
  - May have anchor location (e.g., centroid)

# Types of Spatial Queries

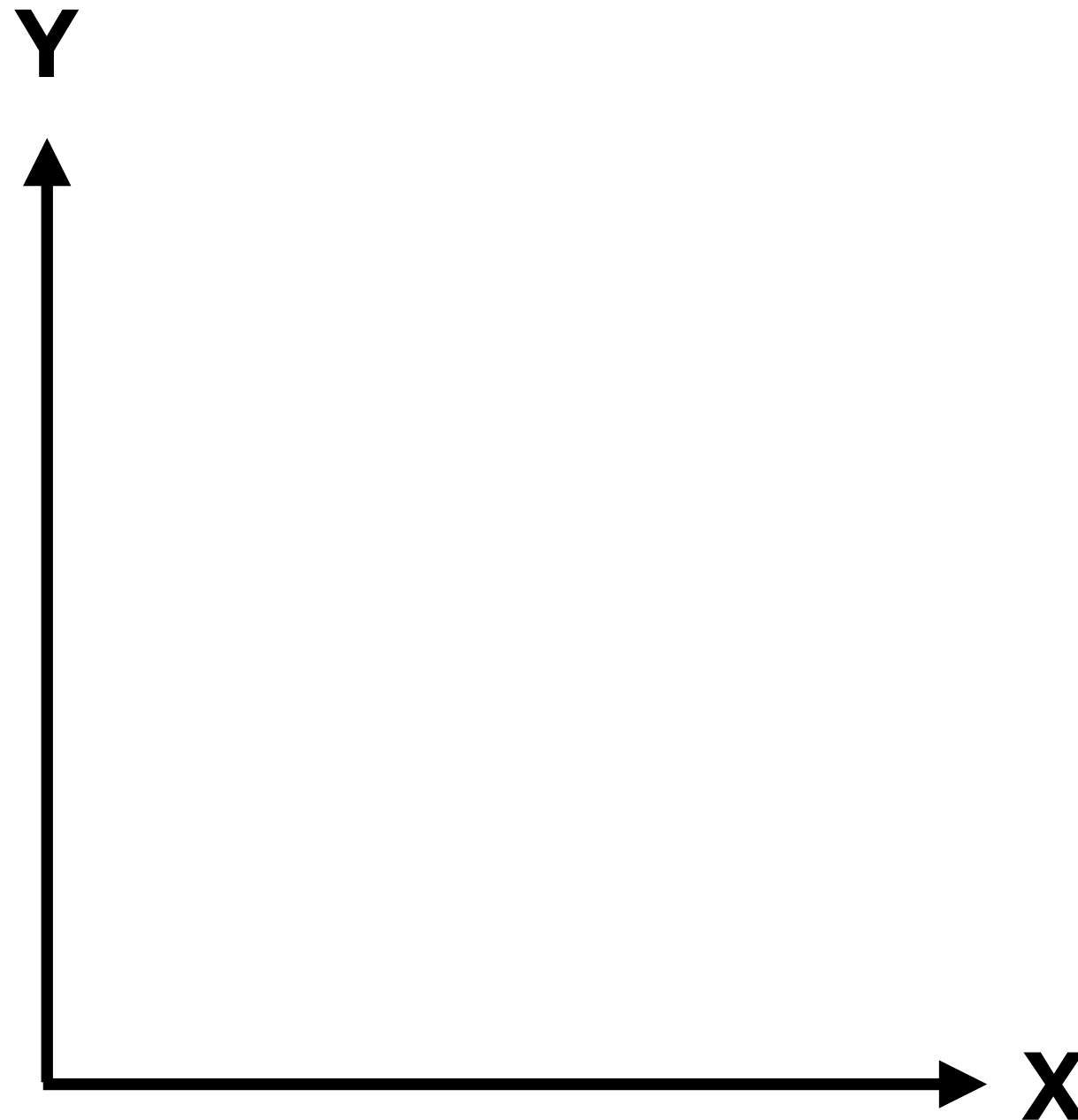
- **Spatial range** queries
  - E.g., show me restaurants in Ithaca
- **Nearest neighbor** queries
  - E.g., show me the nearest gas station
- **Spatial joins**
  - E.g., show hiking trails with parking within 100 m

# Outlook: Indexing

- **B+ trees** for spatial data
- Space-filling **curves**
- **Region** quad tree
- **Grid** files
- The **R tree**

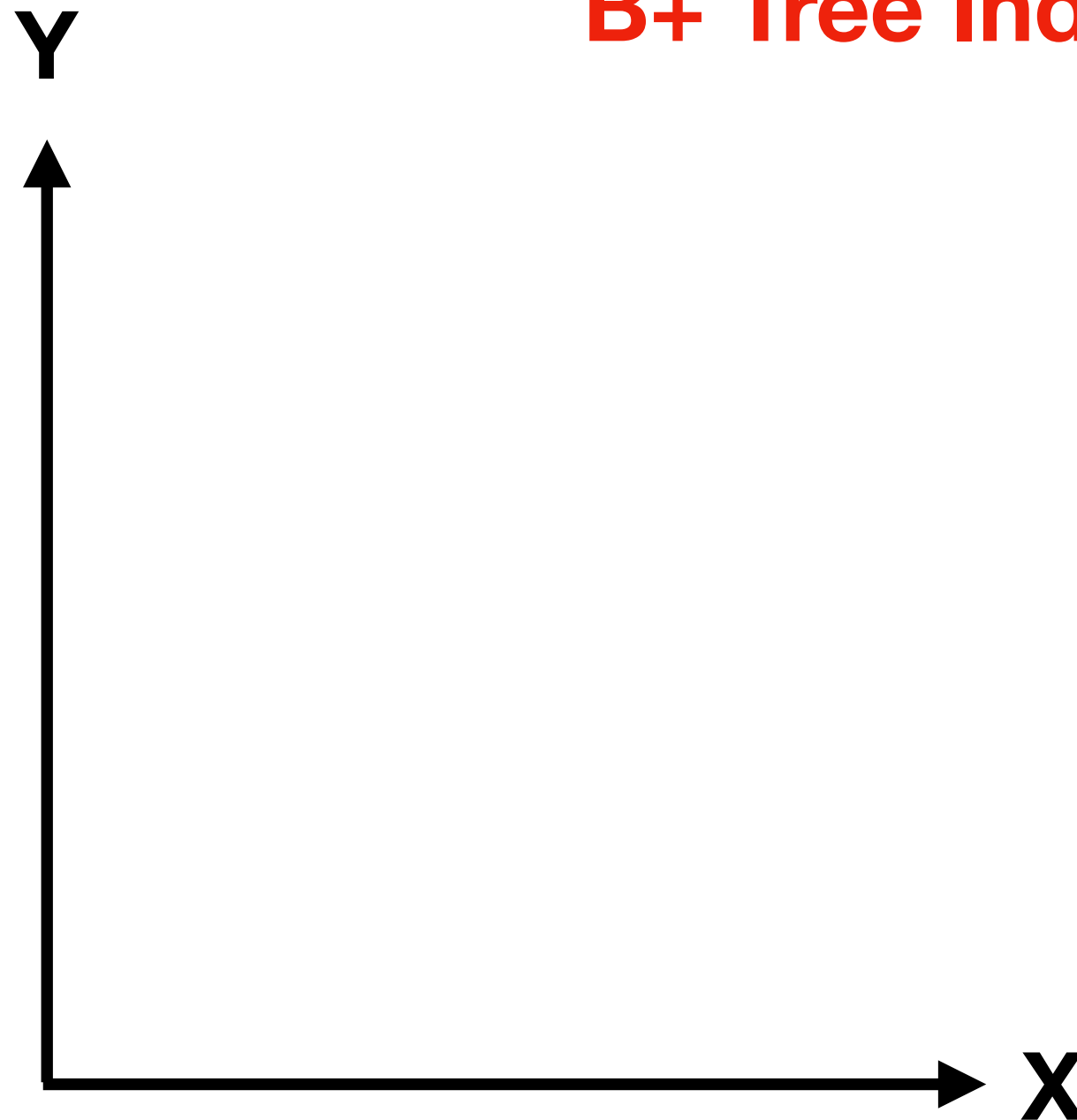


# B+ Trees for Spatial Data

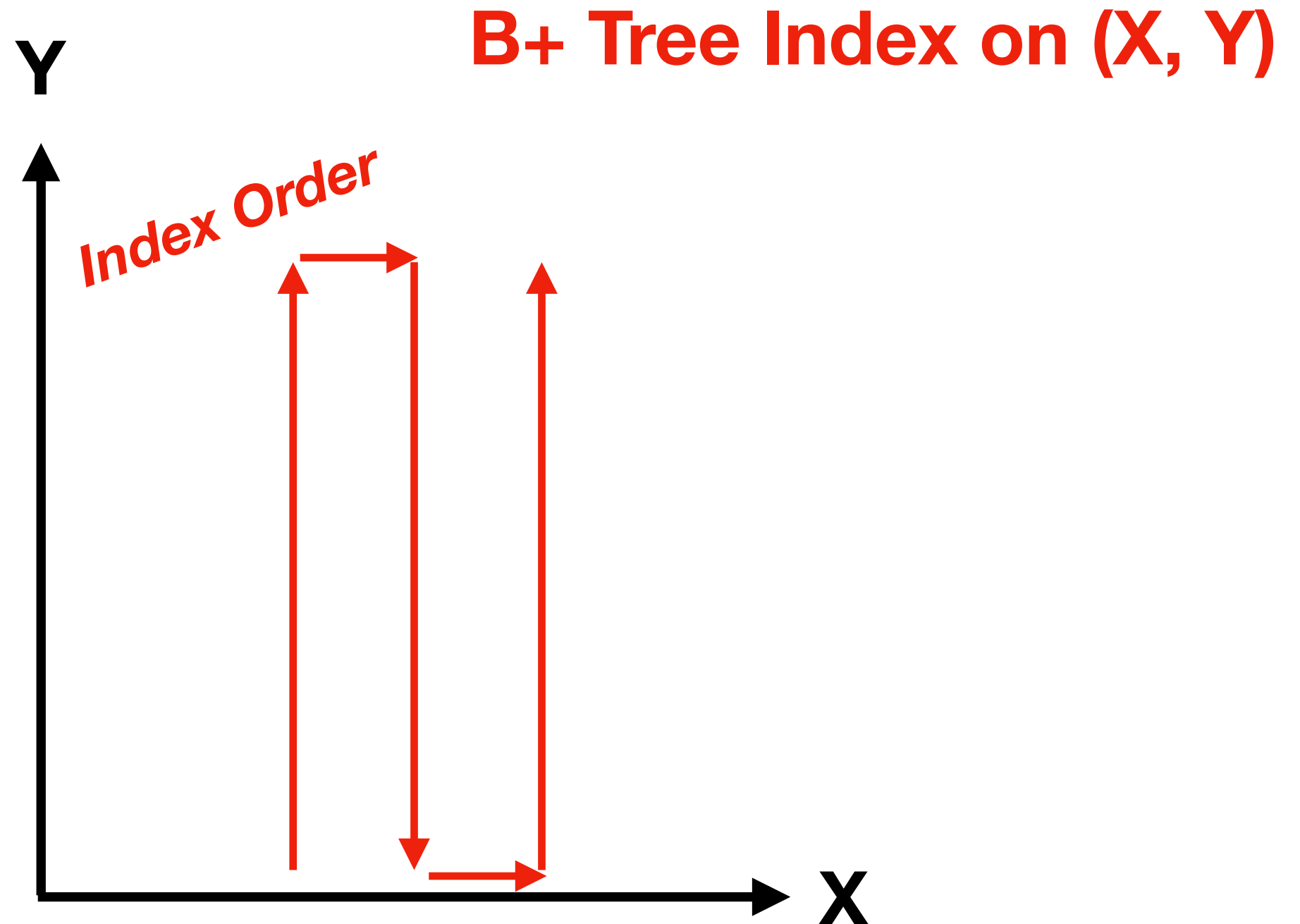


# B+ Trees for Spatial Data

**B+ Tree Index on (X, Y)**

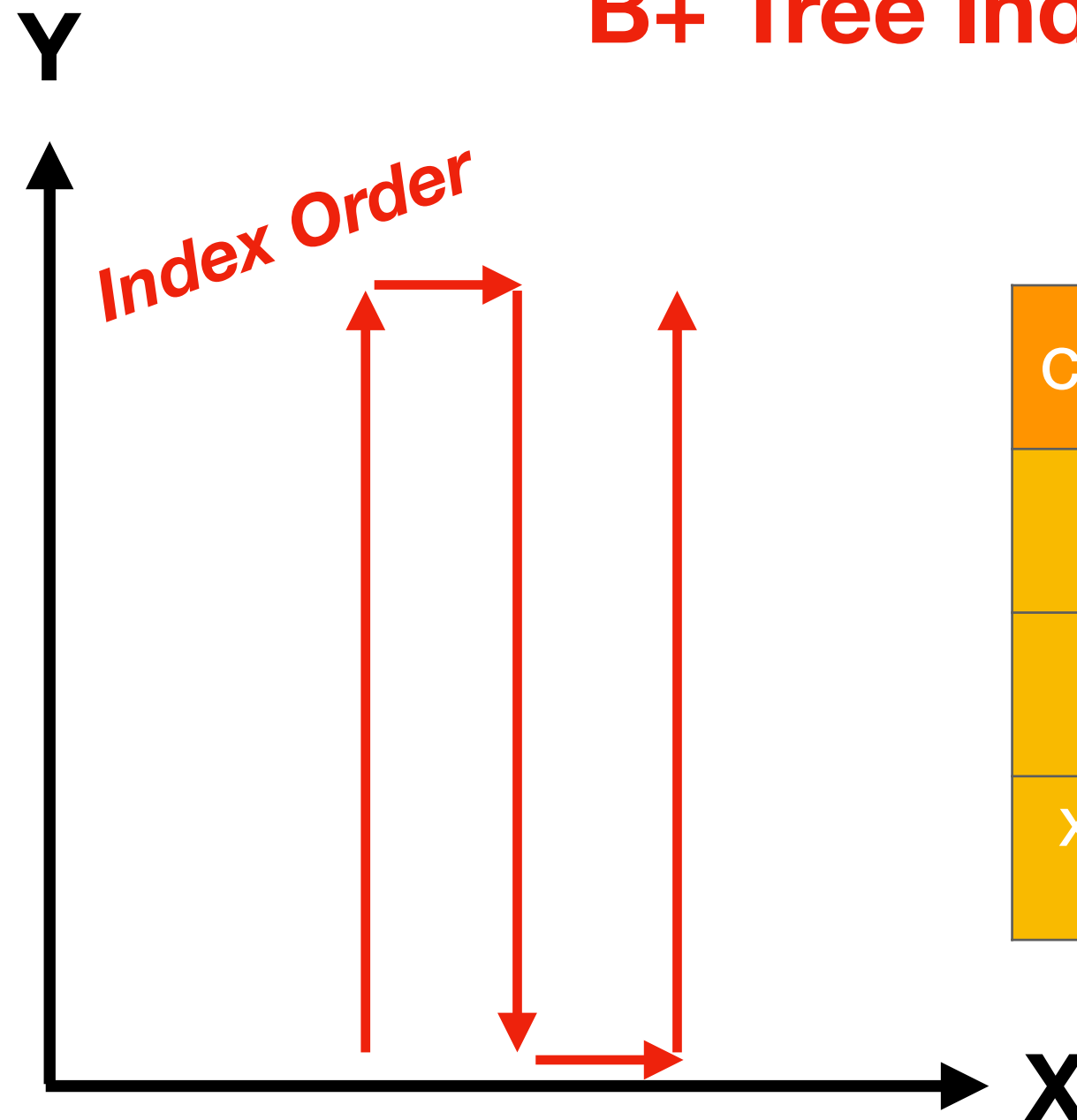


# B+ Trees for Spatial Data



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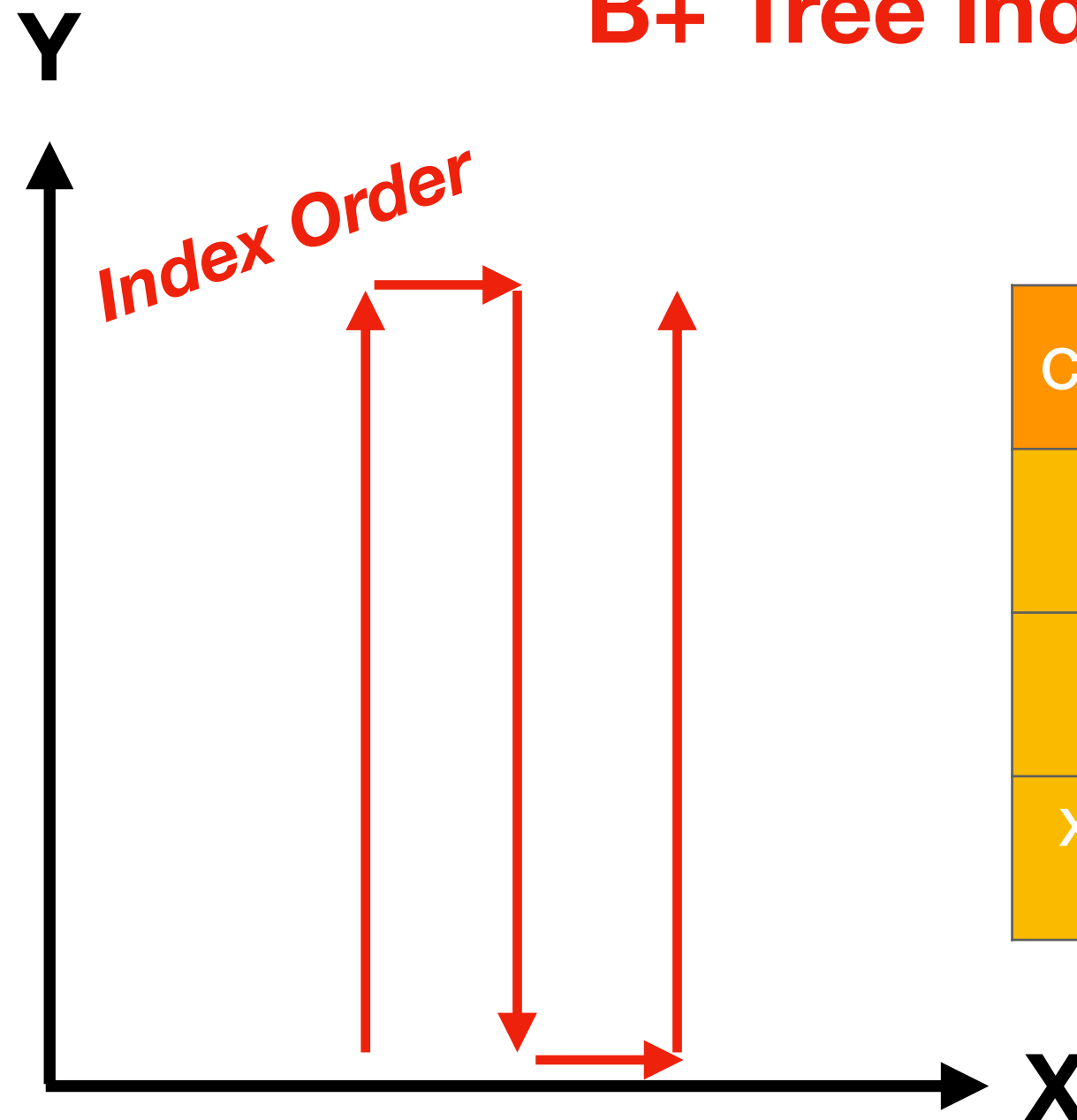
## B+ Tree Index on (X, Y)





Condition	Applicable
$X < 3$	
$Y > 2$	
$X < 2$ AND $Y < 3$	

# B+ Trees for Spatial Data

## B+ Tree Index on (X, Y)



Condition	Applicable
$X < 3$	
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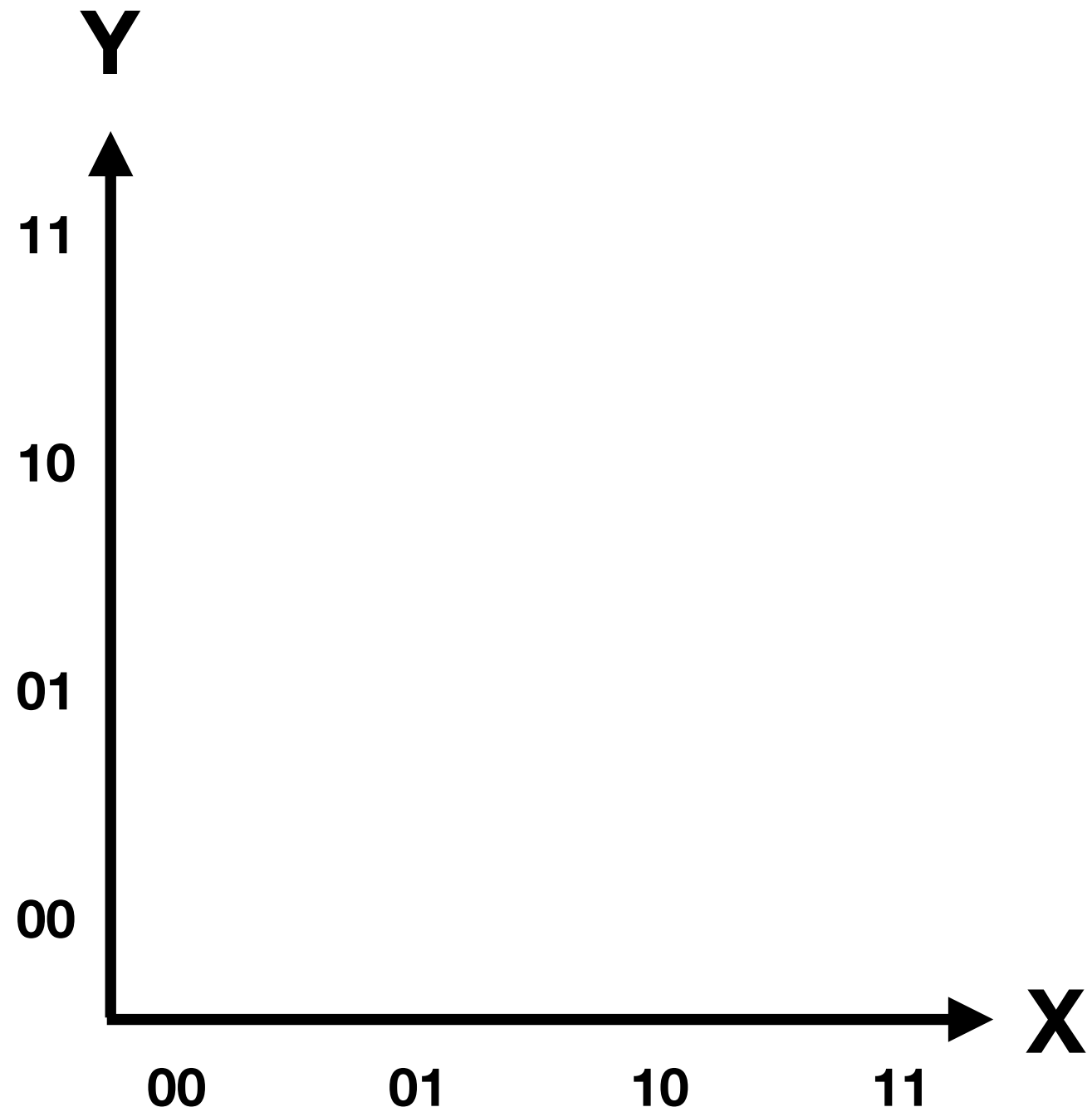
# Problem with B+ Trees

- **Close points** (in 2D) not close in index
- Answering range queries etc. **inefficient**
- Could use one **tree per dimension** and merge RIDs
  - But leads to various overheads!

# Z-Ordering

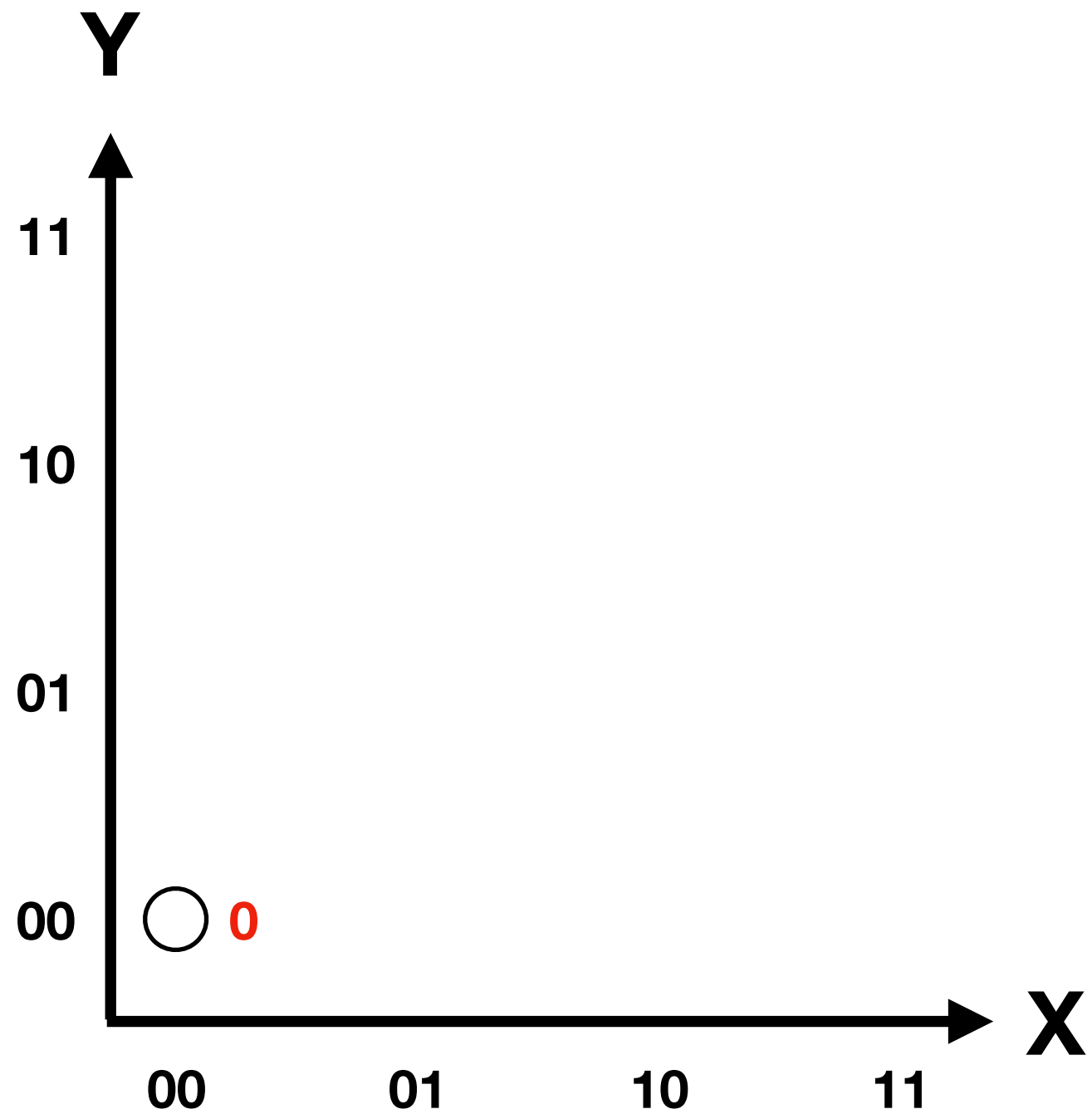
- **Numbers** each space coordinate
- **Close points** have close numbers
  - Not always, can avoid (Hilbert curves)
- **Binary** representation for each coordinate
  - E.g.,  $(a_1a_2...a_n, b_1b_2...b_n)$  for 2D
- Z-Ordering assigns number  $a_1b_1a_2b_2...a_nb_n$

# Z-Ordering

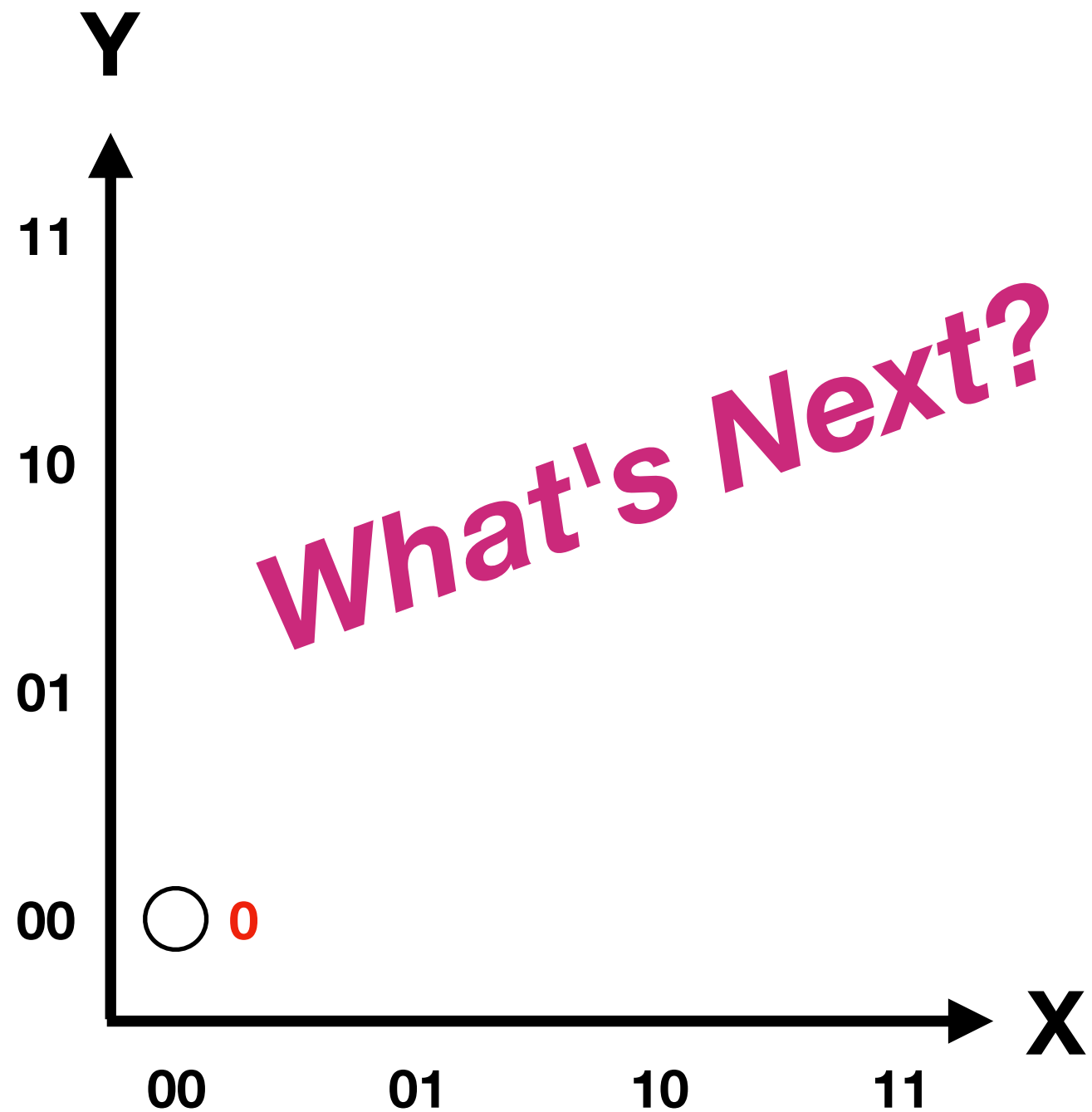




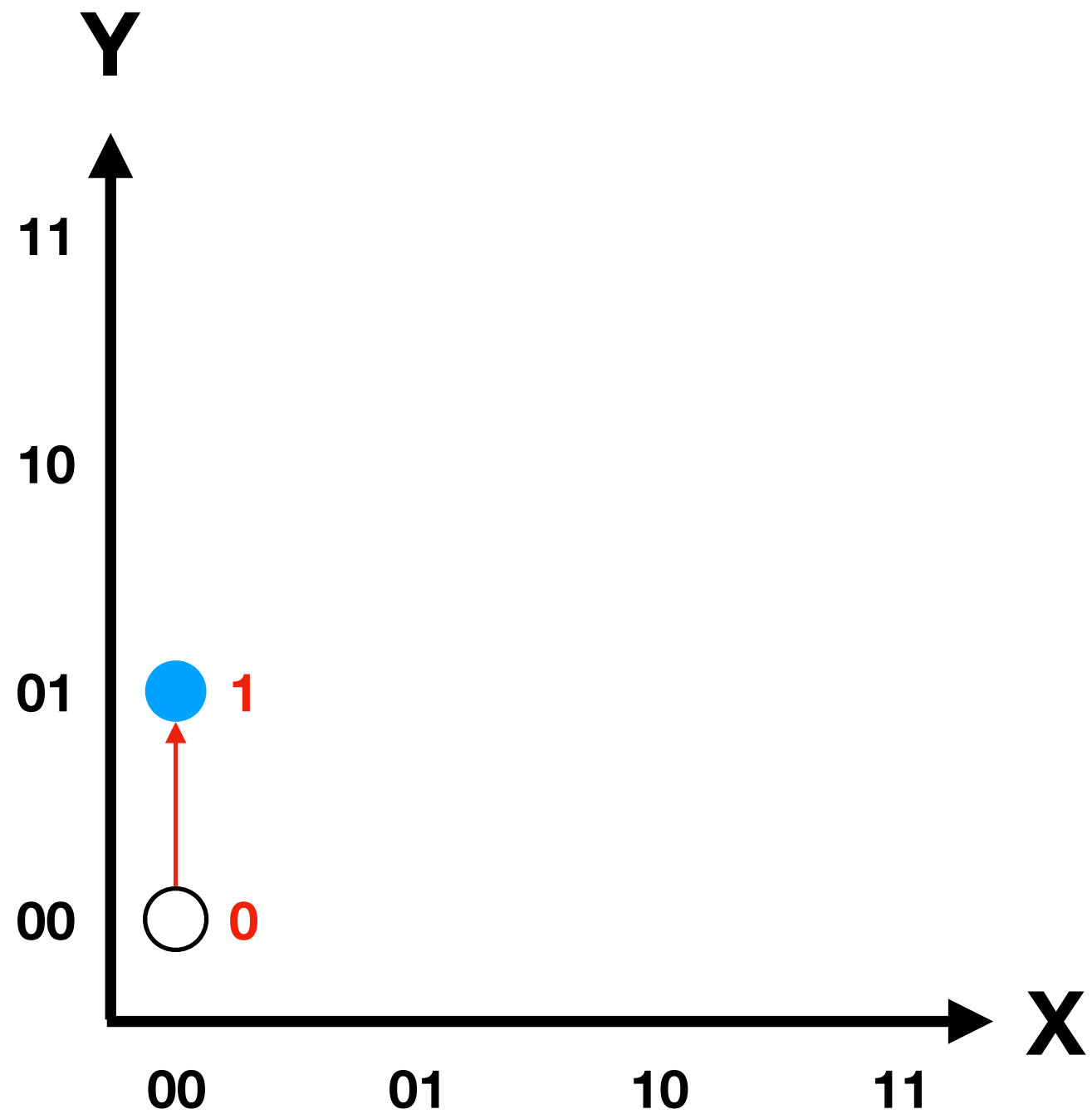
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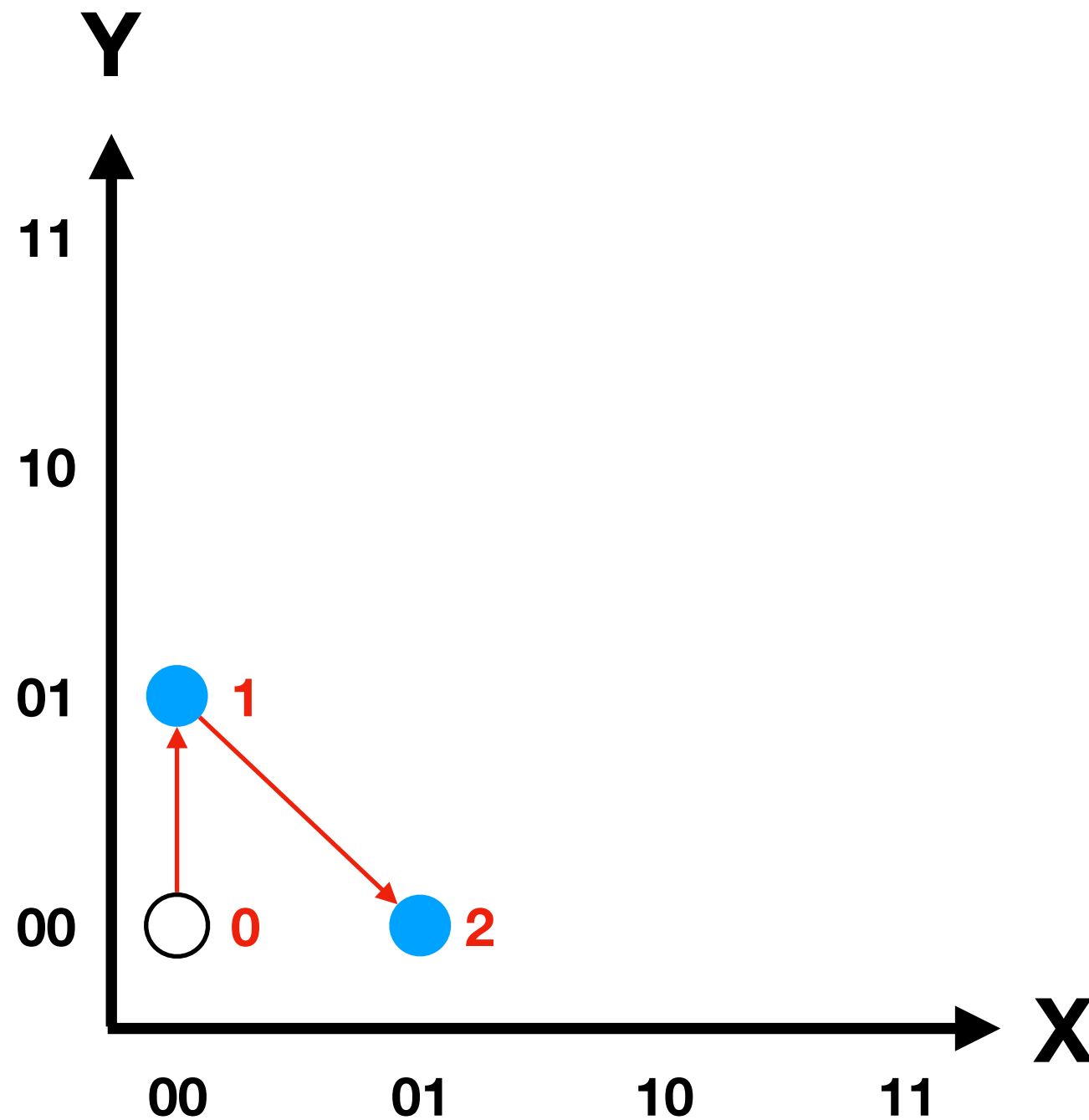
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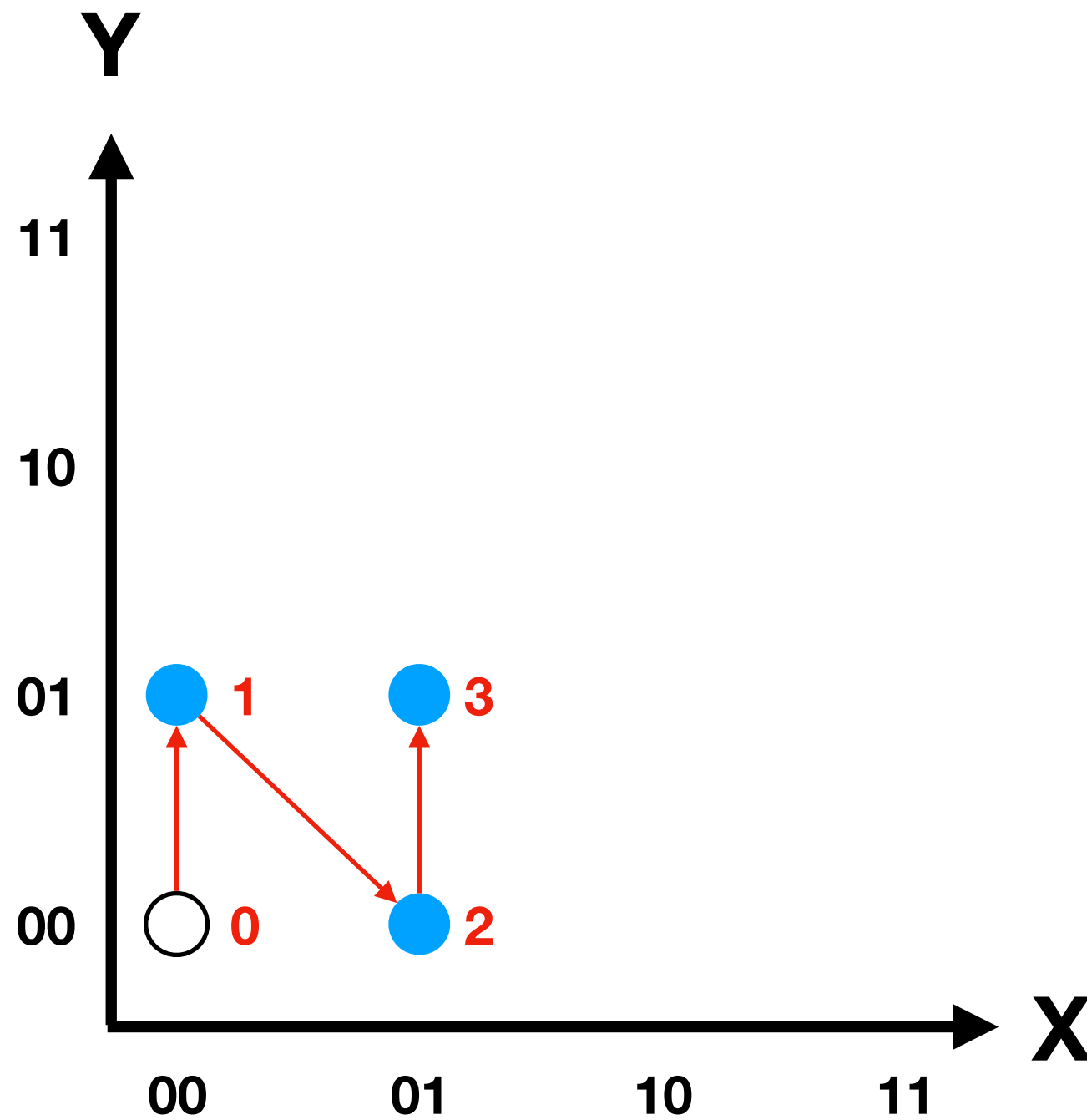
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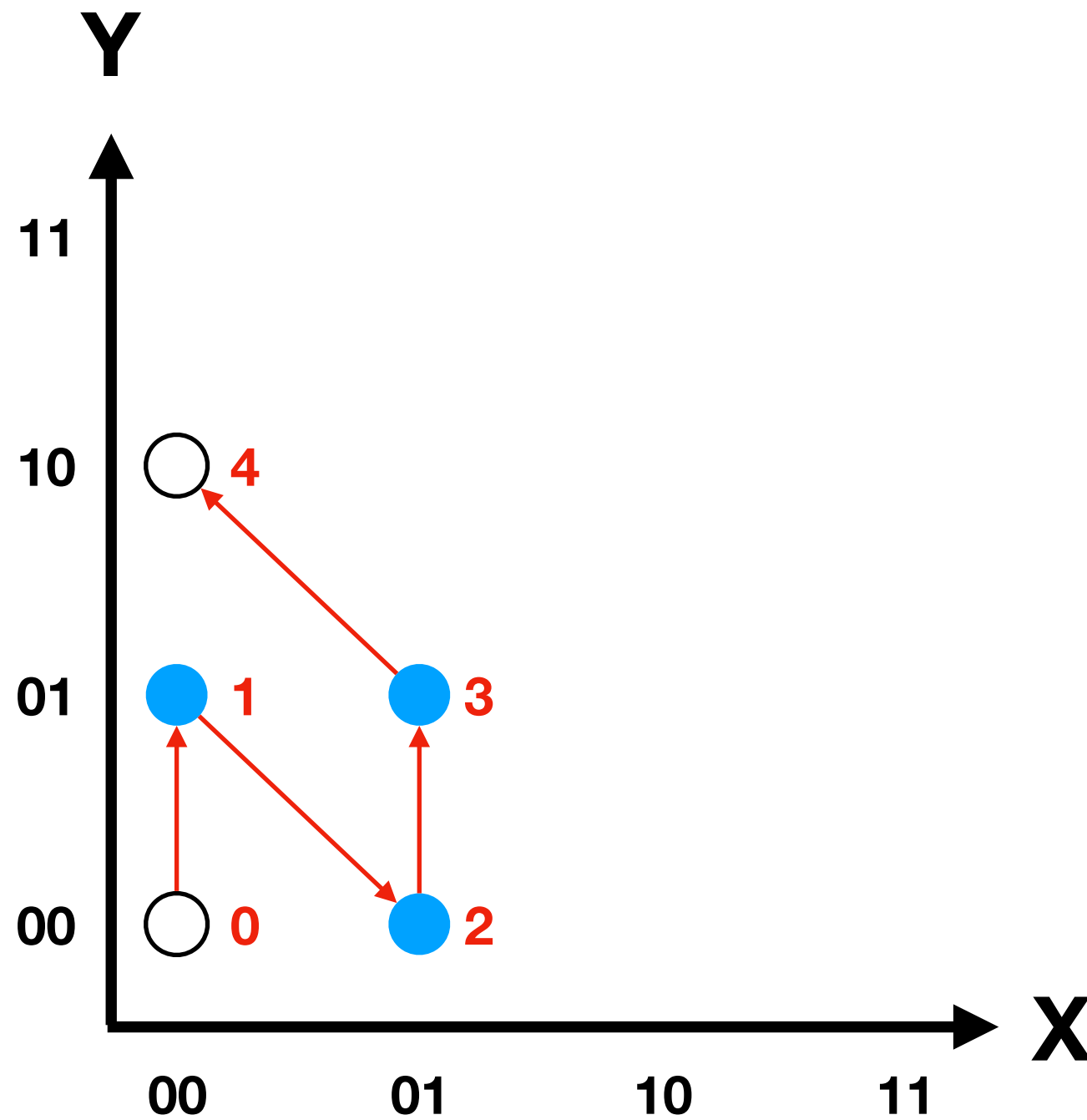
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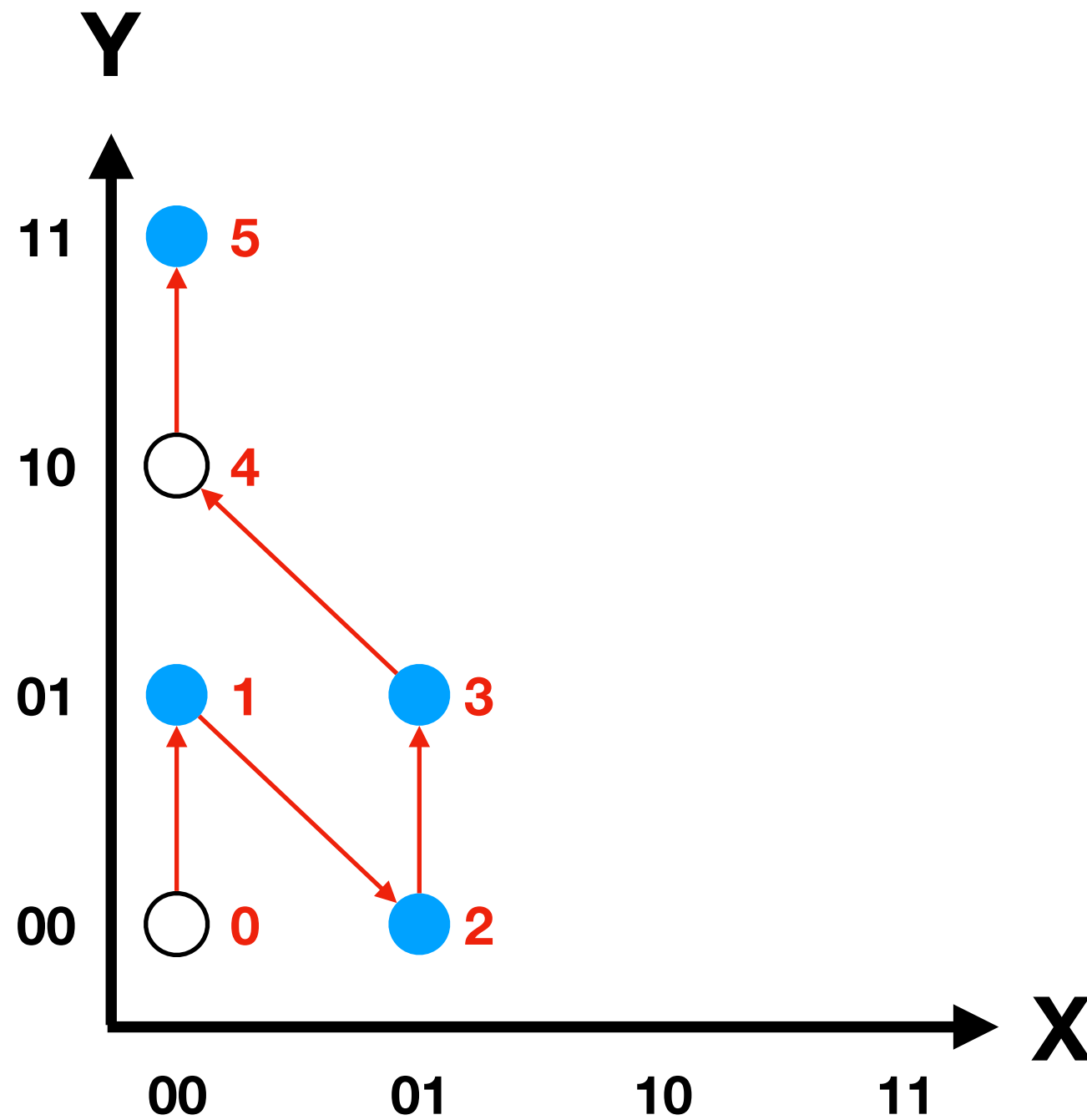
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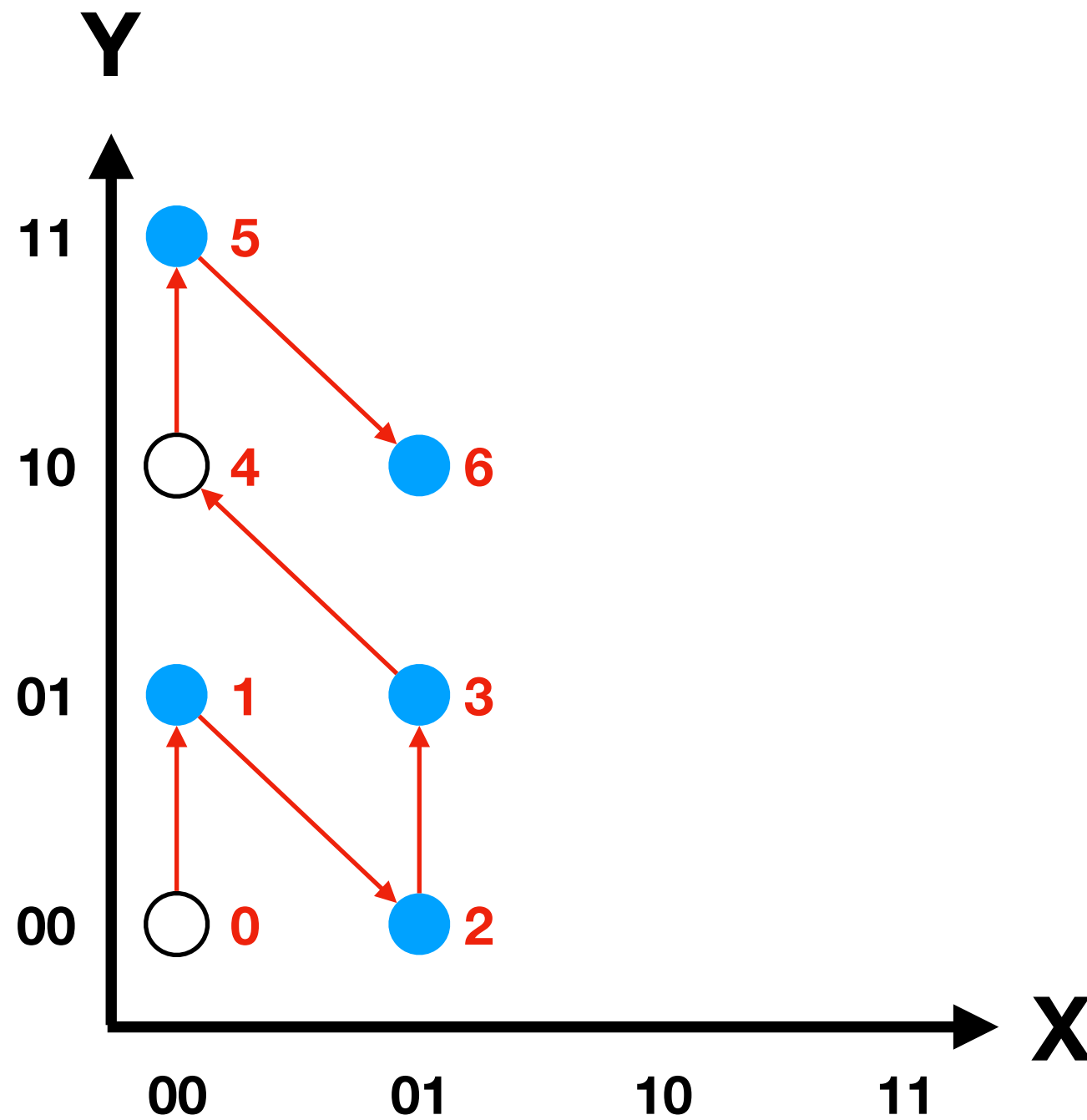
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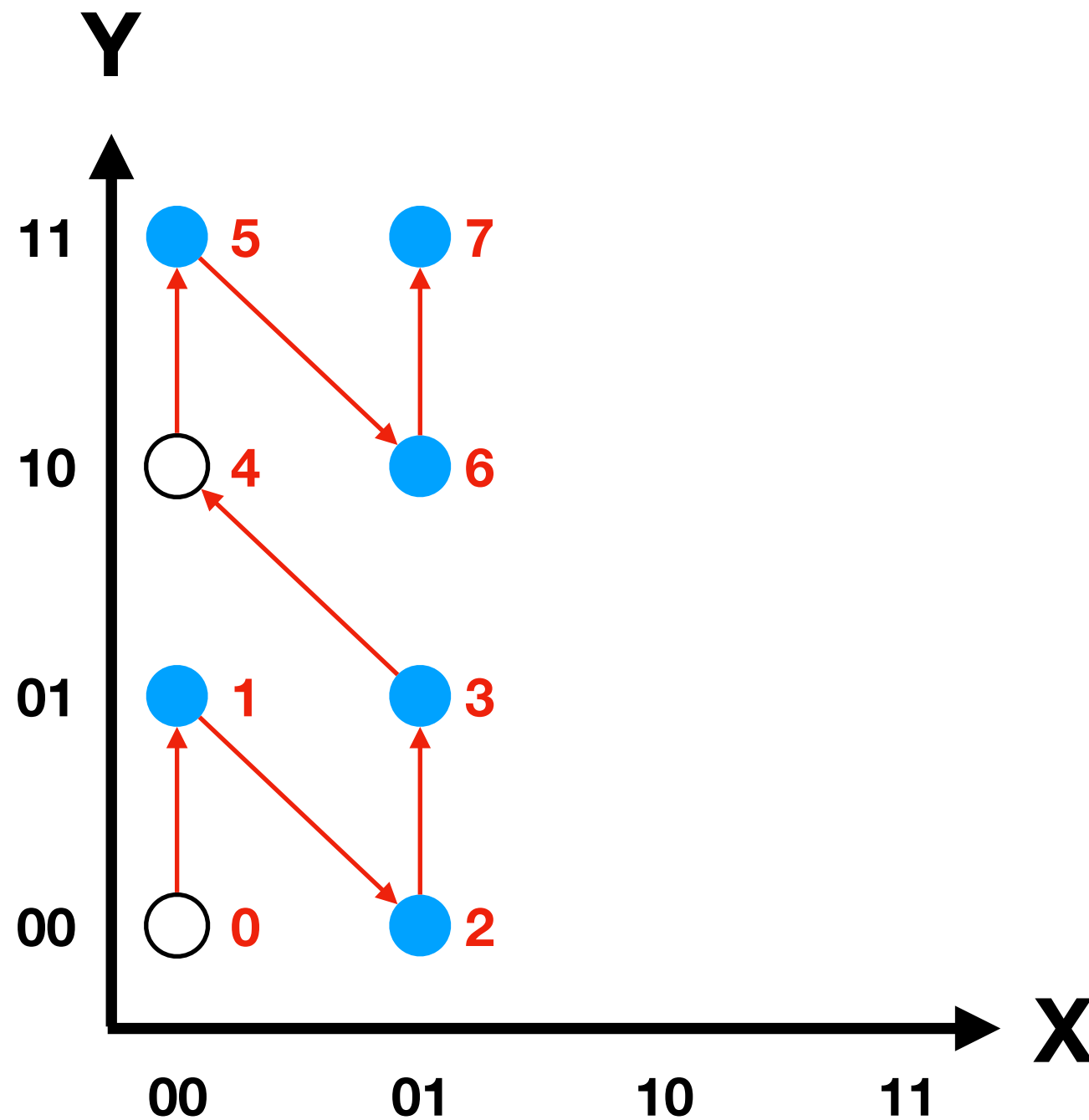


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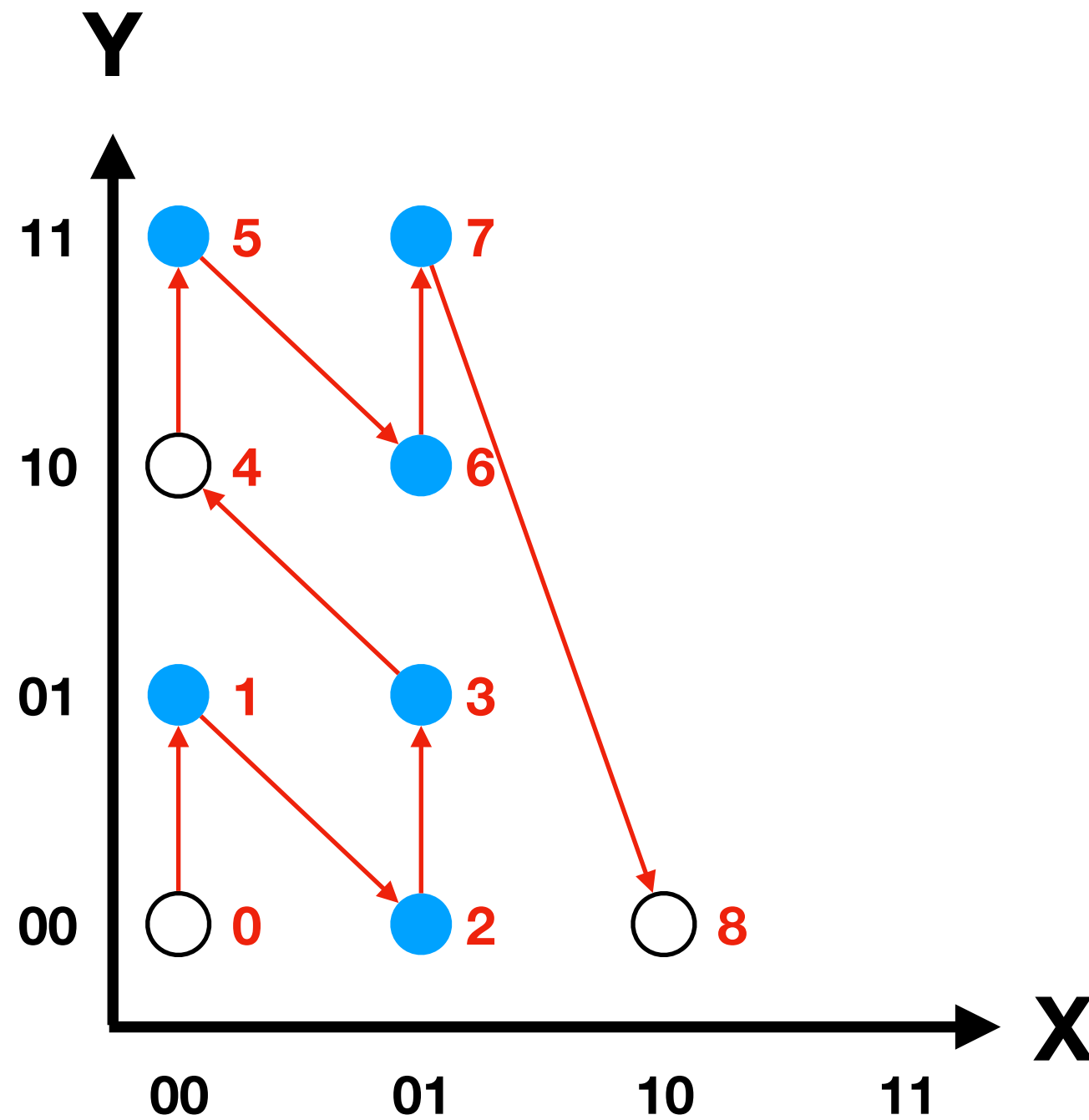




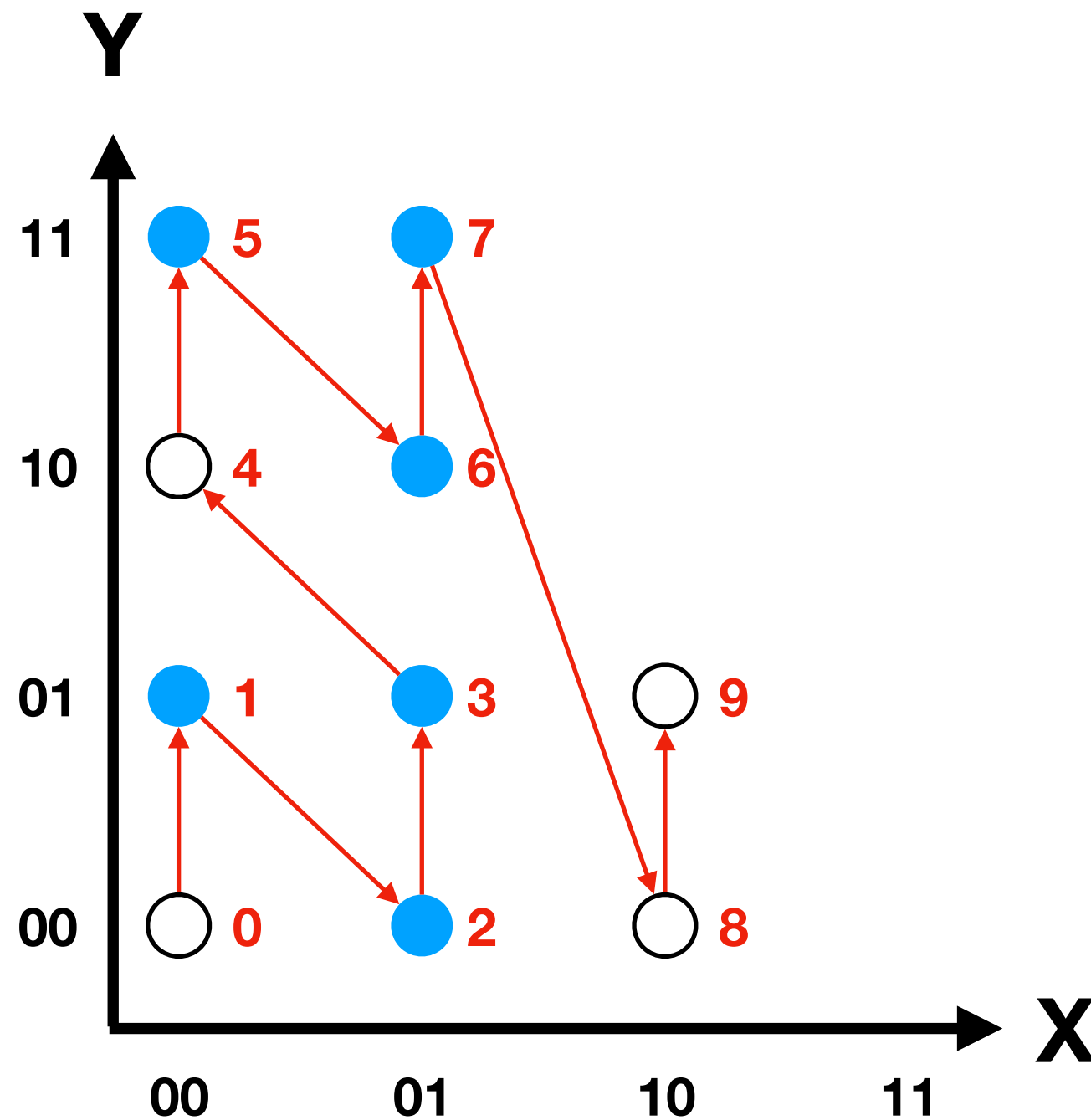
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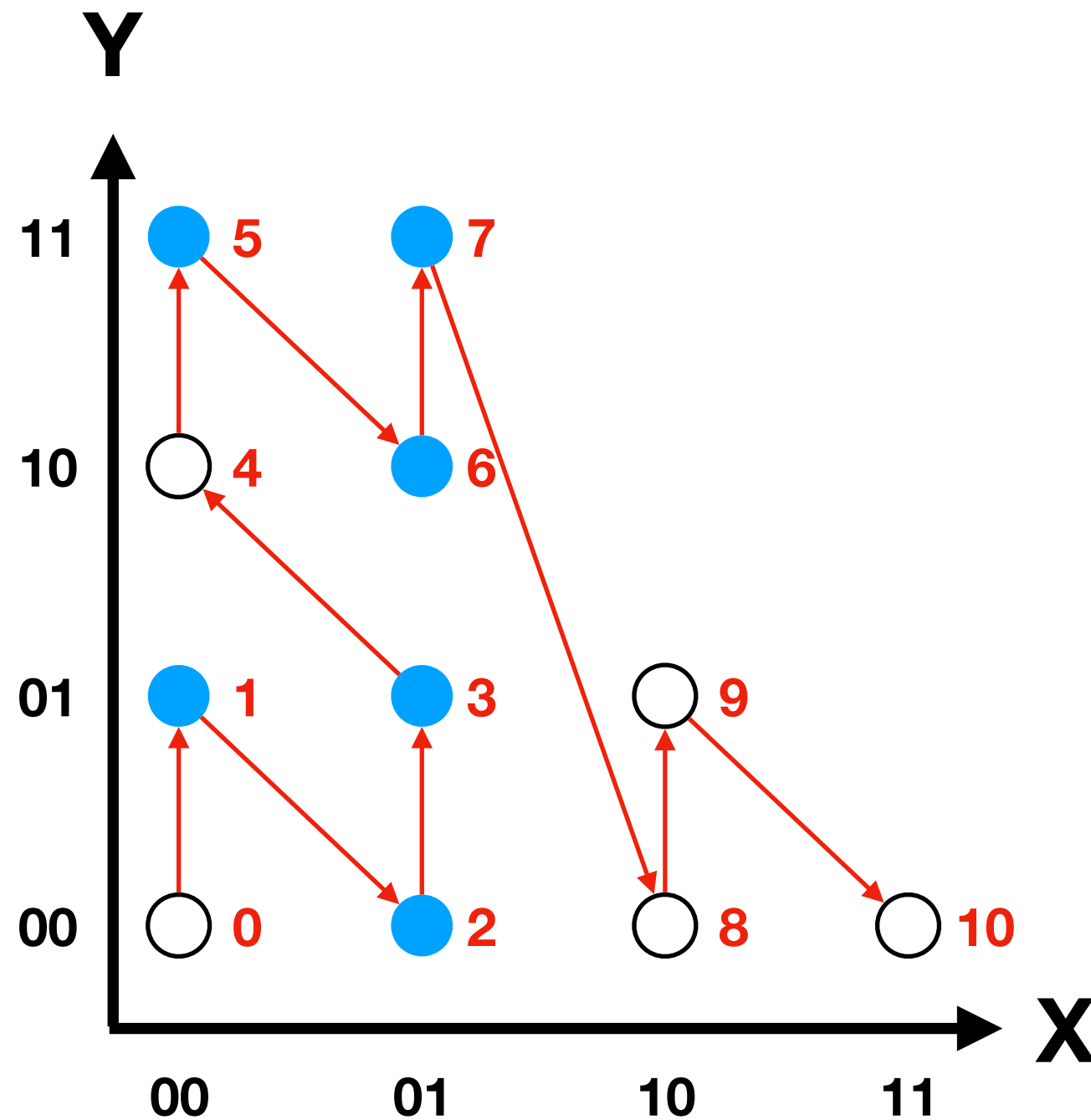
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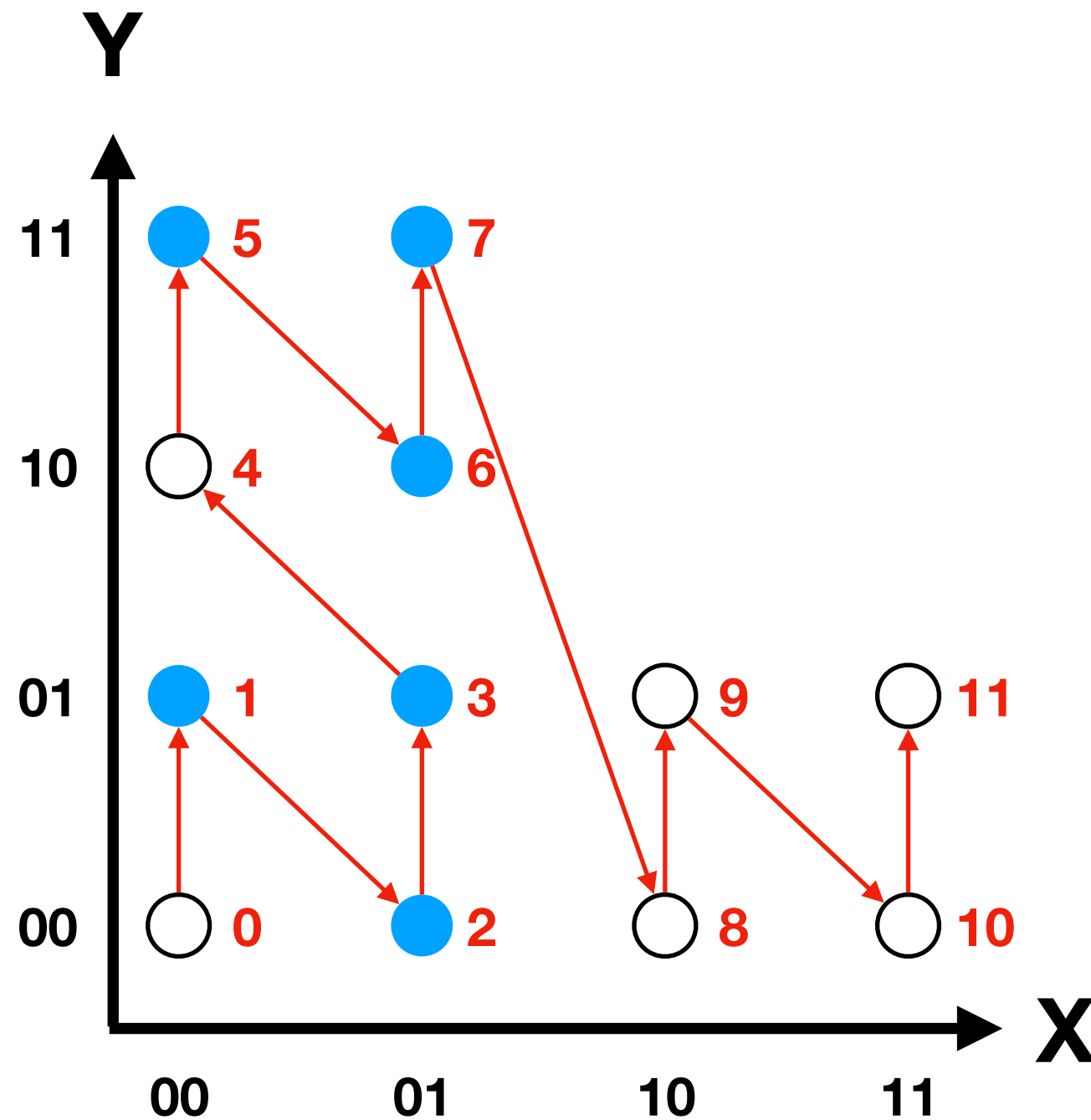
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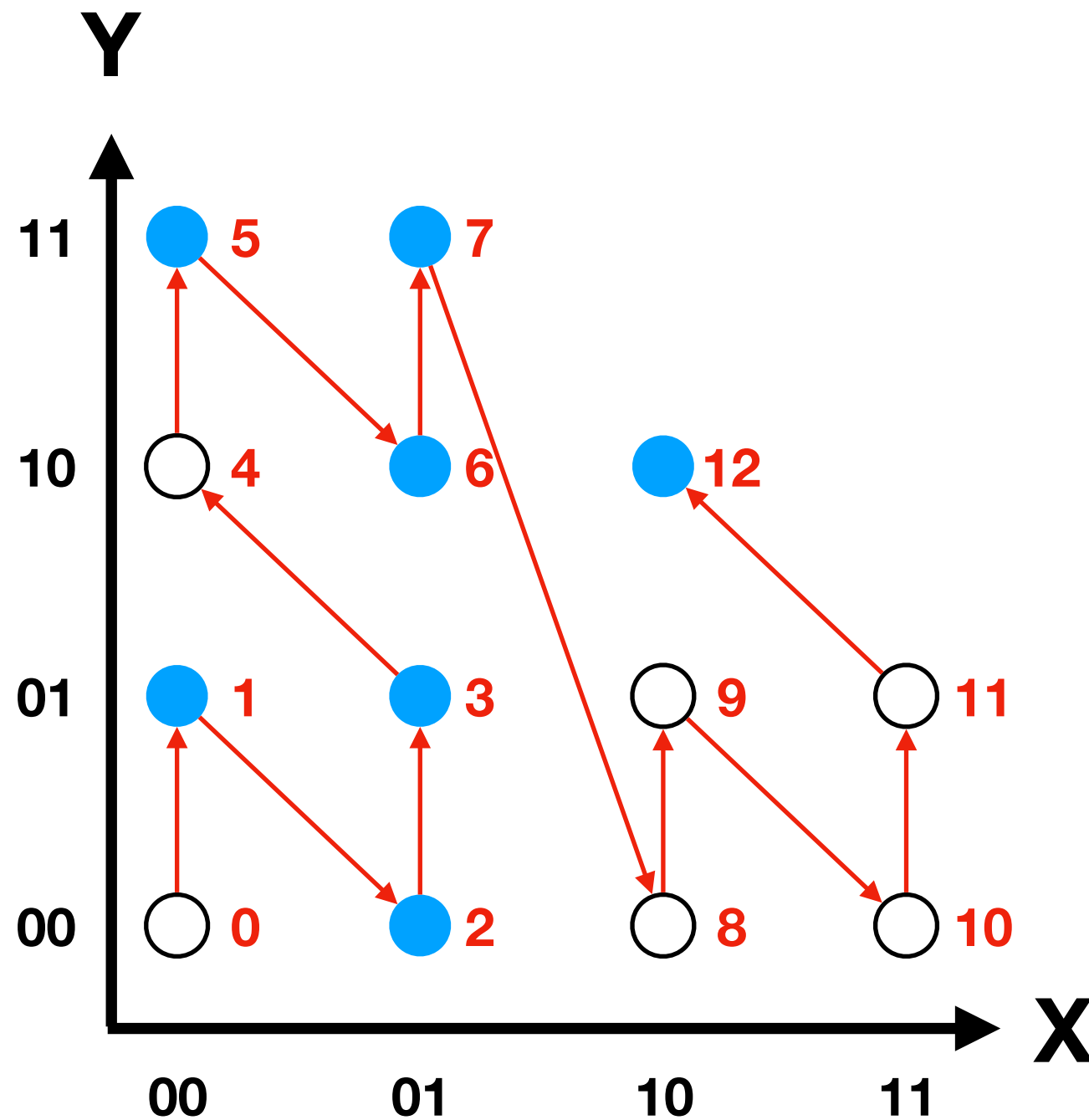
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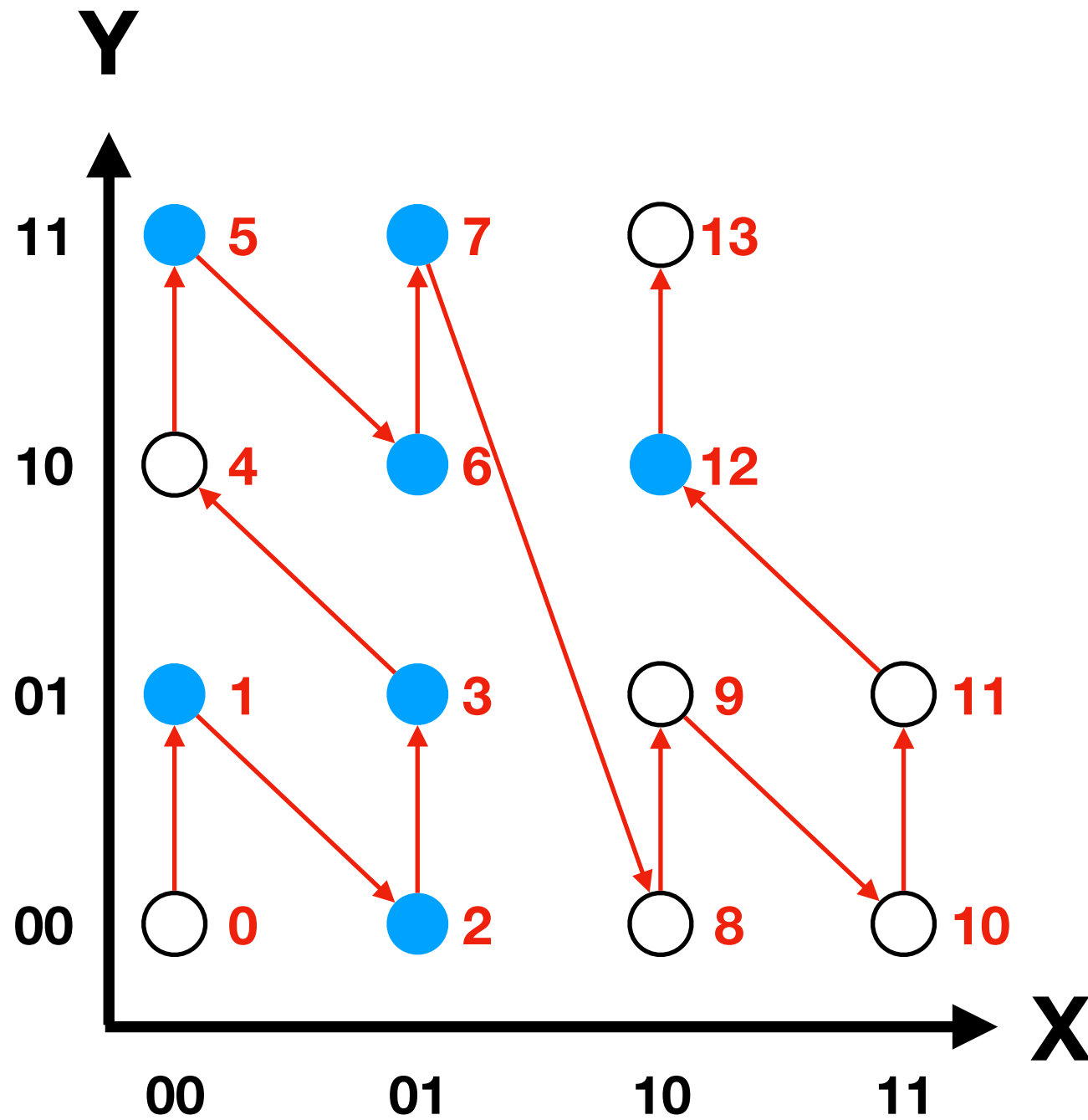
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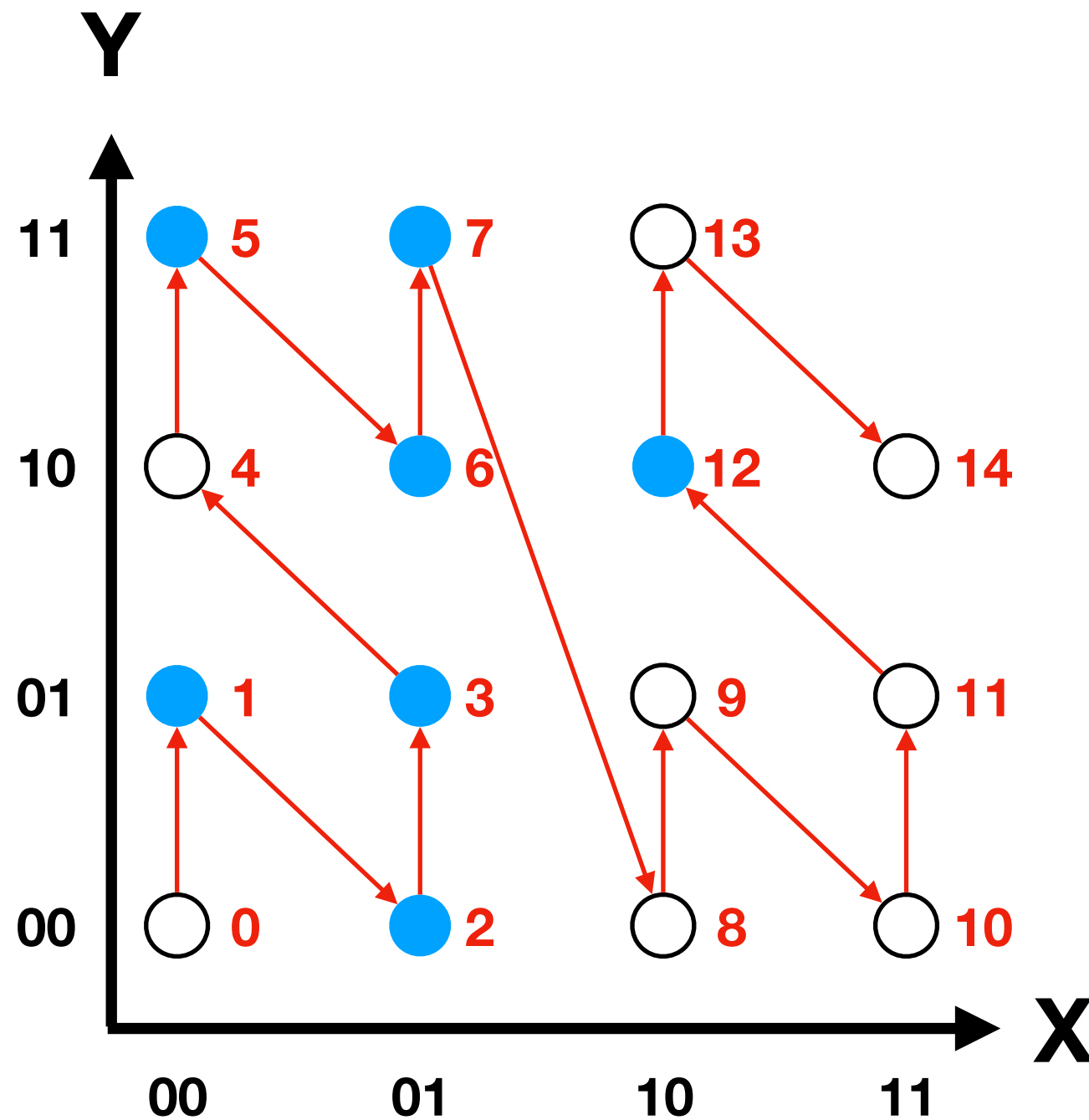
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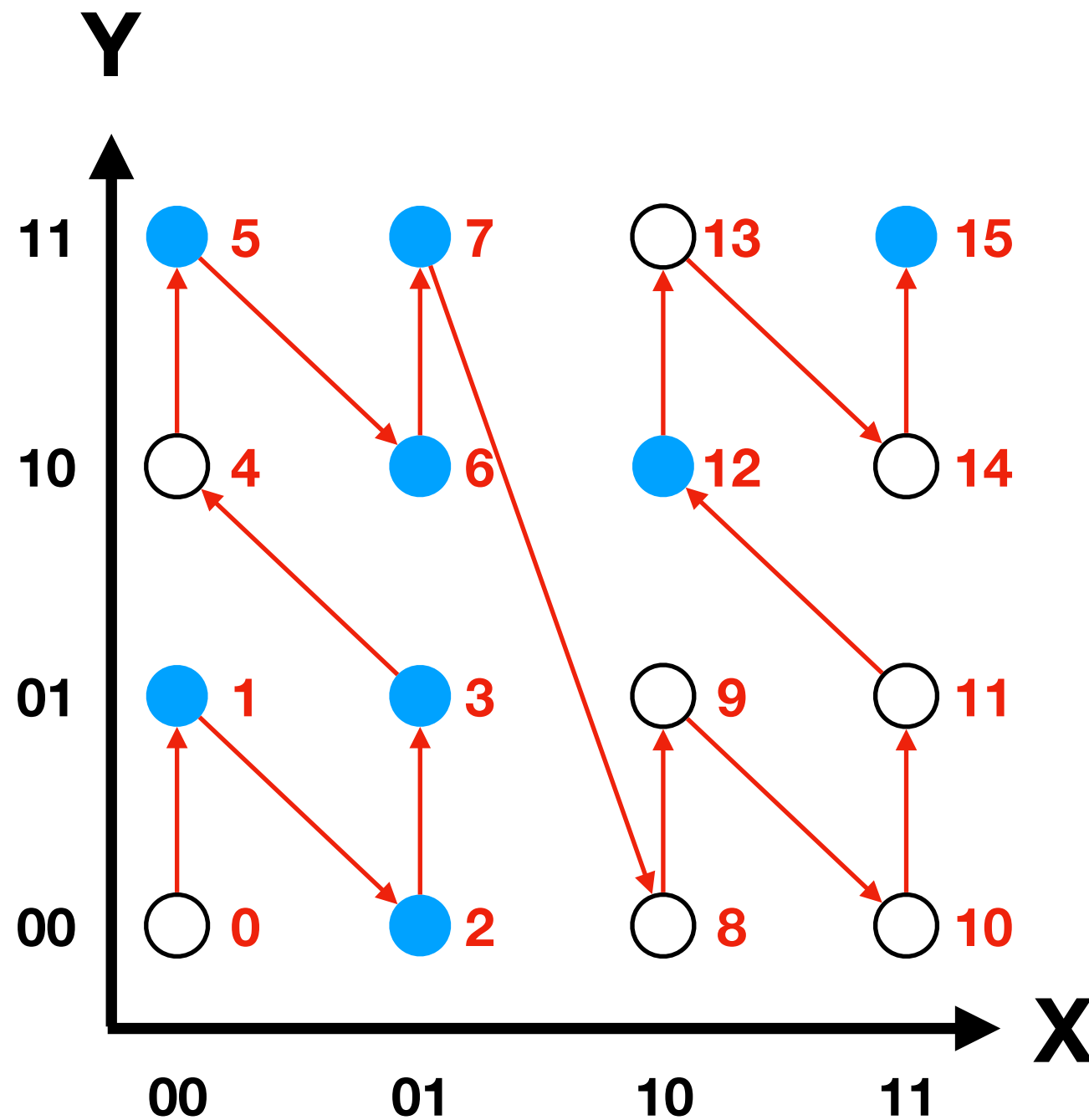


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# Z-Ordering



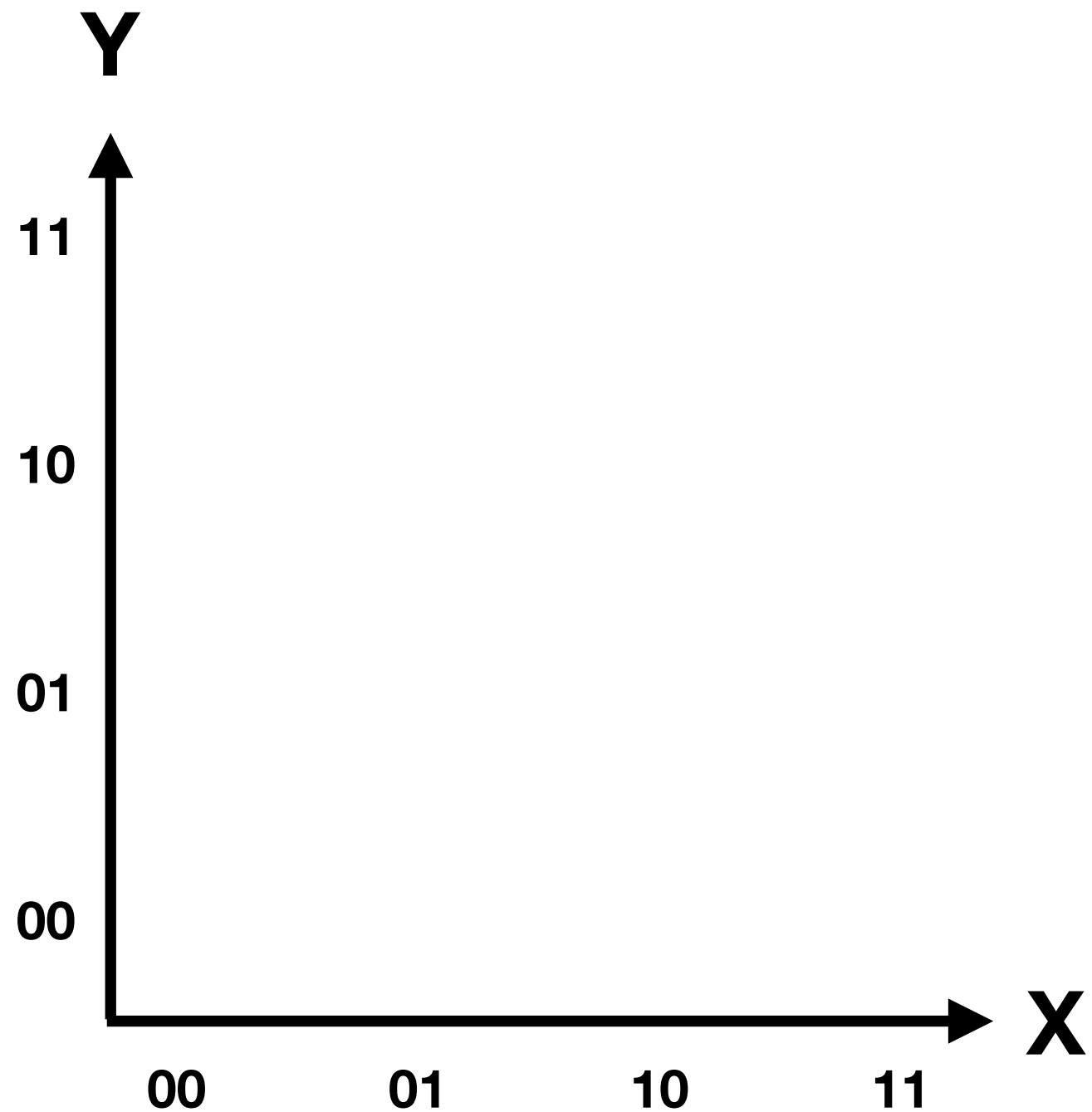
# Indexing with Z-Ordering

- Z-Ordering **reduces** multi-dimensional space to 1D
- Can use **standard index** (e.g., B+ tree) to index Z value
- E.g., translate XD **range queries** to 1D range queries
  - May still require some additional filtering

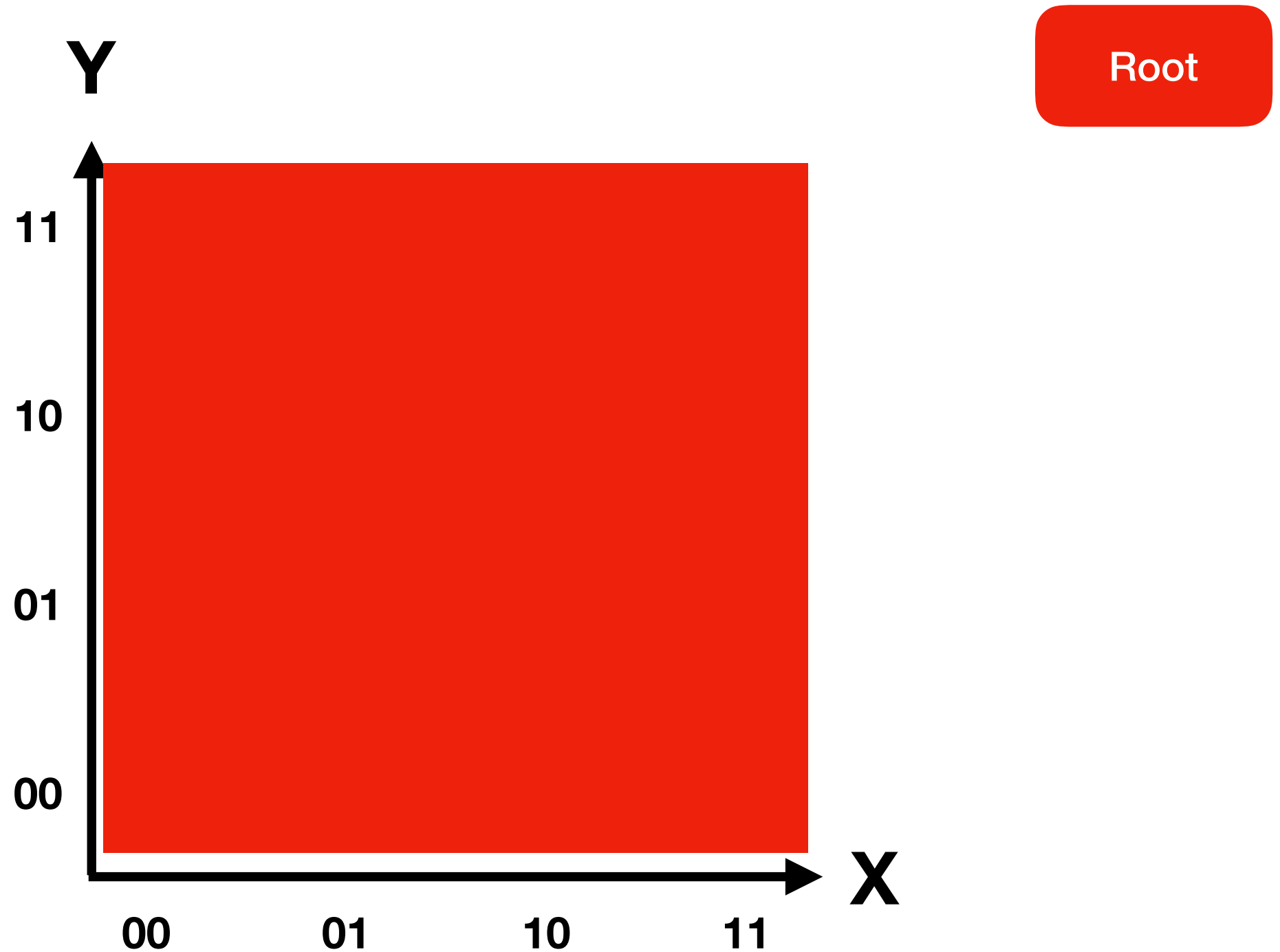
# Region Quad Tree

- Z-ordering enables us to store **points** efficiently
- Storing entire **regions** as set of points is inefficient
- **Region quad trees** divide space recursively
  - In 2D: each region is divided into four quadrants
  - Quadrants are associated with child nodes in tree

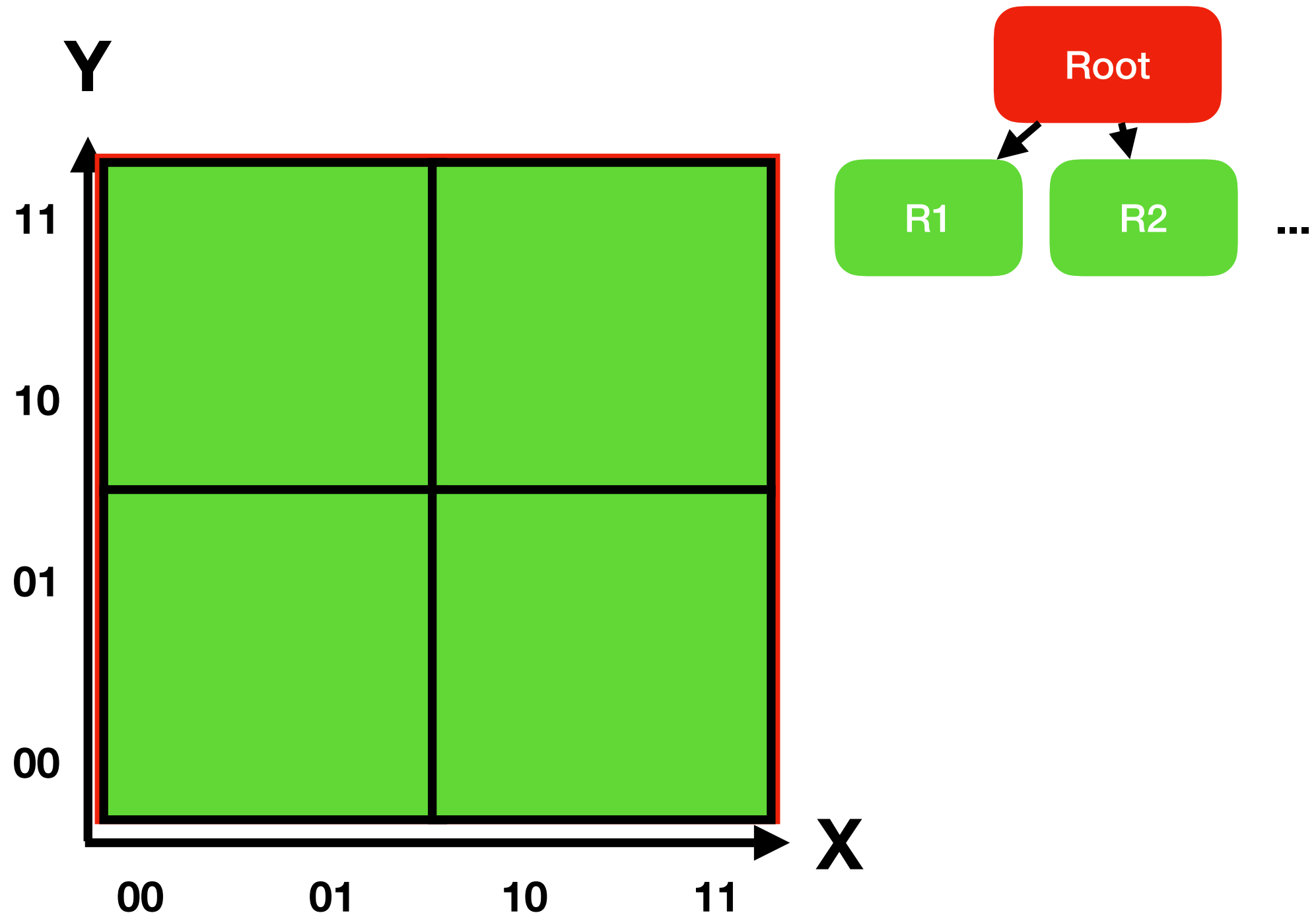
# Region Quad Trees



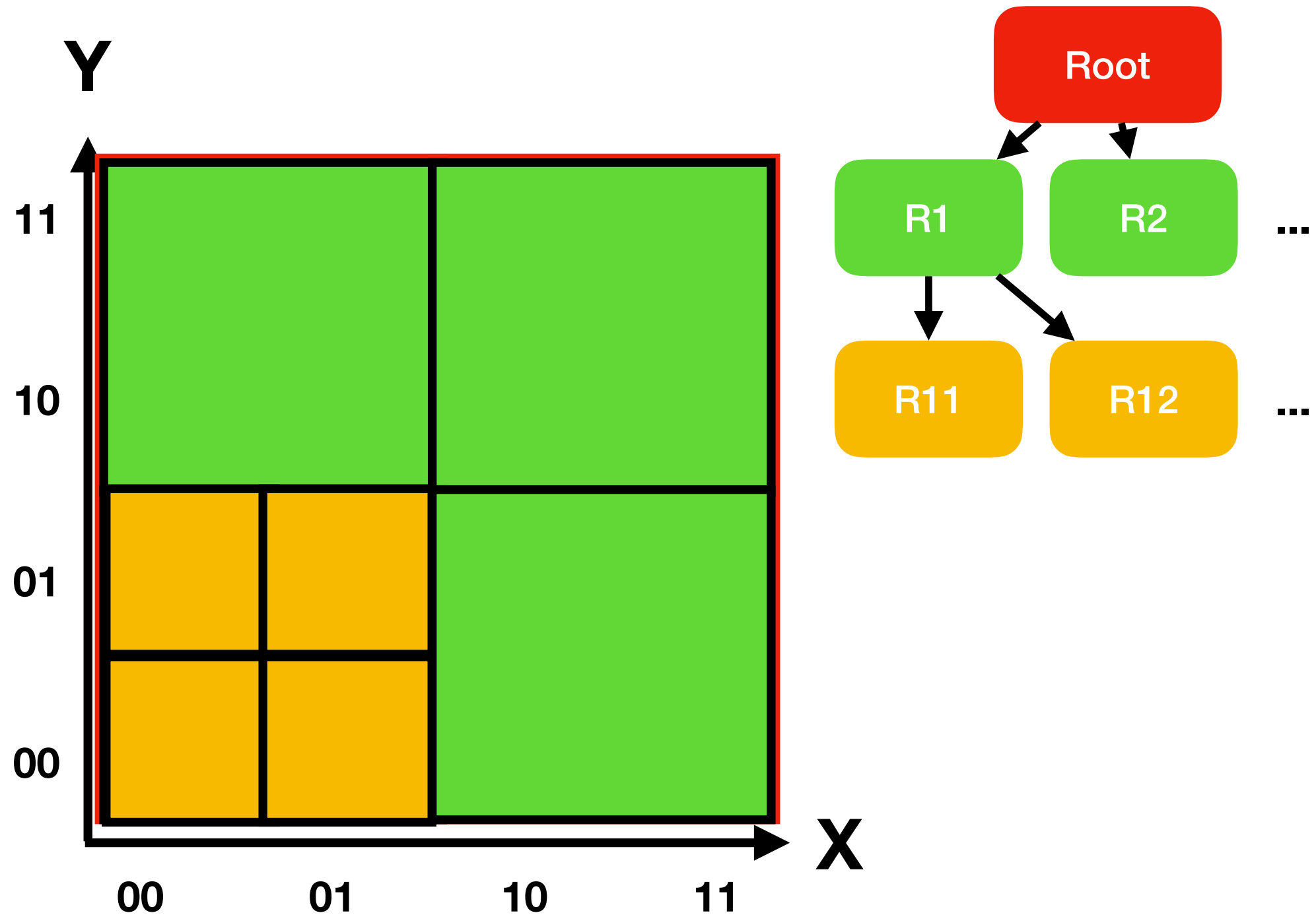
# Region Quad Trees



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# Region Quad Trees



# Grid Files

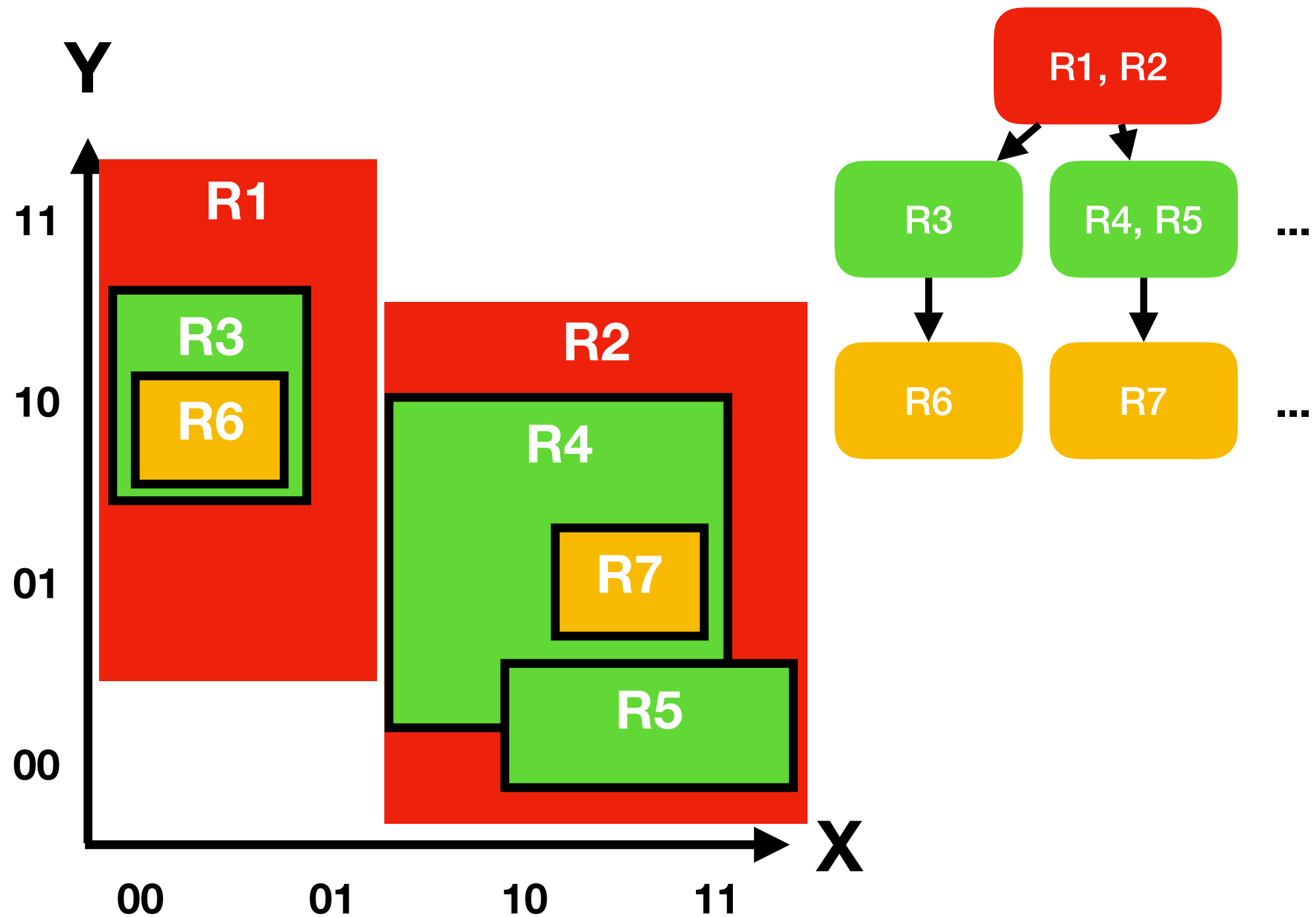
- Region quad trees partition **independently** of data
- This is not optimal if data is highly **skewed**
- Grid files **adapt** space partitioning to data
- More **fine-grained** representation for denser areas
- See **book** for more details



# R Trees

- Adaption of **B+ tree** to handle spatial data
- **Search key**: multi-dimensional bounding box
- **Data entries**: (bounding box, rid)
  - Box is smallest box to contain object
- **Index entries**: (bounding box, pointer to child)

# R Tree Illustration



# R Trees: Lookups

- Compute **bounding box** for query object
  - Can be single point or region
- Start at **root node** of R tree
- Check children **containing** query object
  - May need to check multiple children

# R Trees: Insertions

- Compute **bounding box** for inserted object
- Start at **root** node and proceed to leafs
- Select child needing **minimal extension** for object
- **Insert** object at leaf node
  - May have to **enlarge** bounding boxes on path to leaf
  - May have to **rebalance** the tree

# R Tree Illustration

*How to insert This Object?*

